

A Quality-Centric TCP-Friendly Congestion Control for Multimedia Transmission

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Abstract—In this paper, we propose a quality-centric congestion control for multimedia streaming over wired IP networks, which we refer to as media-TCP-friendly congestion control (MTCC). Our solution adapts the sending rate to both the network condition and the application characteristics by explicitly considering the distortion impacts, delay deadlines, and interdependencies of different video packet classes. The media-aware solution is able to provide differential services for transmitting various packet classes and thereby, further improves the multimedia streaming quality compared to the conventional network-aware congestion control. We use finite-horizon Markov decision process (FHMDP) to determine the optimal congestion control policy that maximizes the long-term multimedia quality, while adhering to the horizon- K TCP-friendliness constraint, which ensures long-term fairness with existing TCP applications. Moreover, the proposed MTCC is able to achieve quality-based fairness among multimedia users. We derive sufficient conditions for multiple multimedia users to achieve quality-based fairness using MTCC congestion control. Note that the proposed solution only modifies the adaptation mechanism of the TCP congestion window size at the sender, without changing the design at the receiver side (i.e., each current TCP receiver can correctly receive and process MTCC streams). Our simulation results show that MTCC achieves more than 3 dB improvement in terms of PSNR over the conventional TCP congestion control approaches, with the largest improvements observed for real-time streaming applications requiring stringent playback delays.

Index Terms—Finite-horizon Markov decision process, quality-based fairness, TCP-friendly congestion control for multimedia.

I. INTRODUCTION

TRANSMISSION control protocol (TCP) is the most widely used protocol for data transmission at the transport layer. However, existing TCP congestion control provides dramatically varying throughput that is unsuitable for delay sensitive, bandwidth intense, and loss tolerant multimedia applications [3], [30] (e.g., real-time video streaming, video-conferencing, etc.). This is due to the fact that current TCP congestion control aggressively increases the congestion window until congestion occurs, and then adopts an exponential backoff mechanism to mitigate the congestion. The

fluctuating throughput results in long end-to-end delays which can easily violate the hard delay deadlines required by various multimedia applications. Hence, numerous multimedia transmission solutions over IP networks adopt User Datagram Protocol (UDP) at the transport layer [27]. However, UDP provides unreliable services without guaranteed delivery, which limits the quality-of-service (QoS) support for multimedia applications at the transport layer. Therefore, multimedia applications need to rely on error resilience [8], forward error correction [9], [10] and/or source coding rate control solutions [11], [27], which need to be implemented at the application layer to achieve a desirable streaming quality. Moreover, the lack of congestion control mechanisms in UDP can lead to severe network congestion. Therefore, a significant body of existing multimedia streaming research over the past decade has focused on applying UDP-based congestion control that are TCP-friendly [4], which are being standardized as the Datagram Congestion Control Protocol (DCCP) [28]. However, these solutions often ignore the specific characteristics and requirements of multimedia applications, thereby leading to a sub-optimal performance for these applications.

Multimedia applications have several unique characteristics which need to be taken into account when designing a suitable congestion control mechanism. First, multimedia applications are loss tolerant, and graceful quality degradation can be achieved when the packet loss is moderately low and multimedia packets having lower distortion impacts are not received. Hence, various scheduling strategies [18], [19] were proposed to optimize the received multimedia quality for multimedia streaming by prioritizing packets for transmission over error-prone IP networks. Such solutions, which explicitly consider multimedia packets' distortion impacts, have also been adopted in order to improve the performance of congestion control mechanisms for multimedia applications [7]. Secondly, multimedia applications are delay-sensitive, i.e., multimedia packets have hard delay deadlines by which they must be decoded. If multimedia packets cannot be received at the destination before their delay deadlines, they should be purged from the senders' transmission buffers to avoid wasting precious bandwidth resources. Third, in order to remove the temporal correlation existing in the source data, multimedia data are often encoded interdependently using prediction-based coding solutions (as in [20] and [21]). This introduces sophisticated dependencies between multimedia packets across time. Hence, if a multimedia packet is not received at the destination before its delay deadline, all the packets that depend on that packet should be purged from the transmission buffer to avoid unnecessary congestion, since these packets are not usable at the decoder side.

Manuscript received April 10, 2011; revised September 21, 2011 and January 21, 2012; accepted January 23, 2012. Date of publication February 06, 2012; date of current version May 11, 2012. The associate editor coordinating the review of this manuscript and approving it for publication was Dr. Pascal Frossard.

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Digital Object Identifier 10.1109/TMM.2012.2187178

A. Limitations of Current Transport Layer Solutions for Multimedia Transmission

Supporting real-time multimedia transmission over wired IP networks is an important yet challenging problem. Various approaches have been proposed to adapt the existing transport layer protocols such that they can better support delay sensitive and loss tolerant multimedia applications. However, most current approaches still exhibit several key limitations.

1) *Multimedia Quality Unaware Adaptation*: Conventional transport layer congestion control approaches are application-agnostic, meaning that they merely attempt to avoid the network congestion by adjusting the sending rates, without considering the impact on the application's performance. For example, many TCP-friendly approaches apply analytical models [2] on the long-term TCP throughput and adapt the sending rate to the periodically updated TCP throughput [3], [4]. These model-based approaches aim to optimize the bandwidth utilization, which may fail to maximize the multimedia application performance (e.g., video quality) since they do not consider multimedia characteristics, such as distortion impact, delay deadline, etc.

2) *Flow-Based Models for Multimedia Traffic Without TCP-Friendliness Consideration*: Various approaches are proposed to adapt multimedia applications to the available TCP throughput by applying rate-distortion optimization [11], forward error coding (FEC) [9], [10], video level switching [30], or frame dropping [25]. These solutions often adopt flow-based models for multimedia traffic that only consider the high-level flow rate (e.g., the average rate and peak rate of the flow/frame [27]). They do not explicitly consider their impact on the other TCP users on the same wired IP network. Such TCP-friendliness consideration is important to avoid congestion collapse of the wired IP network.

3) *Myopic Adaptation*: Prediction/estimation of the network condition is widely used in congestion control mechanisms based on network information feedback, e.g., in [4] and [11]. However, these solutions adapt the congestion window myopically, i.e., based only on the current network condition. Considering the packets' delay deadlines and dependencies in the transmission buffer, the congestion window size not only impacts the immediate multimedia quality, but also impacts the available packets in the buffer for future transmission. Hence, it is important to consider not only the instantaneous multimedia quality, but also how the immediate congestion window size impacts the long-term expected quality in the subsequent time slots. In [12], it was shown that the quality can be improved by allowing temporary violation of the TCP-friendliness, while later compensating the congestion control to maintain *long-term* TCP-friendliness. They proposed a joint source rate control and QoS-aware congestion control scheme. However, this solution only considers multimedia source rates and adopts a heuristic rate-compensation algorithm that cannot optimally determine the required congestion window size.

In summary, a media-aware congestion control mechanism that optimally determines the required congestion window size to maximize the long-term multimedia quality in a look-ahead (foresighted) rather than myopic manner is still missing.

B. Contribution of Our Solution and Paper Organization

In this paper, to overcome the above-mentioned limitations, the proposed media-TCP-friendly congestion control (MTCC) makes the following contributions:

1) *Quality-Centric Packet-Based Congestion Control*: The proposed MTCC congestion control is quality-centric, meaning that it aims specifically at maximizing the received multimedia quality. Instead of applying a flow-based multimedia model, our solution takes into account the distortion impact and delay deadline of each packet, as well as the packets' interdependencies using a directed acyclic graph (DAG) [17]. Importantly, instead of reactively adapting the throughput, the proposed MTCC actively and jointly optimizes the congestion window size as well as the transmission scheduling to provide differential services for different packet classes. Performing this joint optimization is very important in order to maximize the multimedia quality, because the optimal congestion window size depends on the transmission order of the multimedia packets in the transmission buffer.

2) *Foresighted Adaptation Using a Markov Decision Process Framework*: We formulate the congestion control problem using a finite-horizon Markov decision process (FHMDP) framework in order to maximize the expected long-term multimedia quality, under a long-term TCP-friendliness constraint over the subsequent K time slots (i.e., horizon- K TCP-friendliness). Such foresighted planning is essential for multimedia streaming since it can consider, predict, and exploit the dynamic characteristics of the multimedia traffic in order to optimize the application performance over dynamic IP networks. We show that the complex FHMDP formulation can be decomposed into multiple optimal stopping problems [23]. Based on the structural results obtained from the decomposition, we present low-complexity threshold-based algorithms when the multimedia packets are coded either independently or interdependently.

3) *Quality-Based Fairness Among Coexisting Streams*: Preserving the fairness among the coexisting streams represents an important issue [1], [6], [29]. However, even though the throughput/bandwidth is equally shared by the users, multimedia users can still experience very different qualities since various applications and source data may result in different traffic characteristics. Hence, instead of the throughput-based fairness proposed by most existing congestion control solutions, we focus in this paper on quality-based fairness. We show that the proposed MTCC is able to achieve quality fairness among multimedia users. In [25], the authors also proposed a frame dropping scheme for min-max distortion fairness. However, the frame dropping approach is determined myopically, without considering the resulting TCP-friendliness to other flows.

In Table I, we compare the features of the proposed MTCC with the existing TCP-friendly congestion control solutions for multimedia streaming.

The paper is organized as follows. In Section II, we first formulate the packet-based MTCC congestion control problem for one MTCC user. In Section III, we present the FHMDP framework used by the MTCC user to determine the optimal trans-

TABLE I
COMPARISONS OF CURRENT CONGESTION CONTROL SOLUTIONS FOR MULTIMEDIA STREAMING

	Name of the adopted congestion control	Type of TCP-Friendliness	Multimedia support	Distortion impact consideration	Delay deadline/Content dependency	Decision type
Towsley 2008 [5]	TCP-streaming	TCP	Playback buffering	No	No	Myopic
Bohacek 2003 [6]	TCP	TCP	Playback buffering	No	No	Myopic
Rejaie 1999 [13]	RAP	AIMD-based	Source rate adaptation – layered encoding	No	No	Myopic
Mark 2005 [14]	DTAIMD	AIMD-based	Optimal source rate is bounded due to buffer underflow at the receiver	No	No	Myopic
Balk 2004 [30]	VTP	AIMD-based	Source rate adaptation – source switching	No	No	Myopic
Seferoglu 2009 [10]	TFRC/FEC	Model-based	Application layer FEC	Yes	No	Myopic
Zakhor 1999 [8]	TFRC	Model-based	Source rate adaptation – packet size adaptation	Yes	No	Myopic
Zhang 2001 [11]	MSTFP	Model-based	Source rate adaptation – distortion minimization s.t. rate budget	Yes	No	Myopic
Our approach	MTCC	Model-based	Quality-centric congestion control	Yes	Yes	Foresighted

mission scheduling and congestion window size. In Section IV, we investigate how to decompose the FHMDP problem and provide structural results for solving this problem in different transmission scenarios. In Section V, we investigate multiple MTCC users interacting in the same network with regular TCP users and discuss the quality-based fairness among the multimedia users. Simulation results are shown and discussed in Sections VI and Section VII concludes the paper.

II. MTCC CONGESTION CONTROL PROBLEM FOR ONE MTCC USER

A. Transport Layer Model

As in TCP, each packet transmission is acknowledged after a round-trip time (RTT) Rtt . Packet loss rate p can be measured based on the packets' acknowledgements. We assume a model-based congestion control as in [4], [8], and [11] that adapts the congestion window size to a long-term available TCP throughput calculated from the packet loss rate p and the round-trip time Rtt (the adaptation will be discussed in Section II-D). Let ℓ represent the packet size. The long-term available TCP throughput can be approximated by $R_{AIMD}(a, b, Rtt, p) = (\ell \sqrt{(2-b)a/Rtt} \sqrt{2bp})$ (bits/sec) [14], where the TCP congestion control is modeled as a special case of generic additive increase multiplicative decrease (AIMD) based congestion control with parameters (a, b) [14]. By substituting (a, b) to $(1, 0.5)$, we have the well-known TCP response function $R_{TCP}(Rtt, p) = (\ell/Rtt) \sqrt{3/2p}$ (bits/sec). We assume a time-slotted system and set the time slot duration T as Rtt . For simplicity, we assume a fixed RTT (time slot) in this paper. Denote the measured packet loss rate in time slot k as p^k . We define the *expected TCP window size* in time slot k as $W_{TCP}^k(p^k) = R_{TCP}(Rtt, p^k)(Rtt/\ell) = \sqrt{3/2p^k}$ (pkts/time slot), which can be viewed as a metric describing the network congestion in time slot k .

B. Application Layer Multimedia Model

Multimedia data is encoded into multiple data units at the application layer. A data unit usually encapsulates a video slice,

which contains a set of macroblocks or an entire video frame (see, e.g., the H.264 standard [21]), which can be packetized into various numbers of fixed-size RTP packets. We assume that these data units are classified into M multimedia classes $\{CL_1, \dots, CL_M\}$ (in this paper, we take video as an example; in fact, audio can be considered in one of such multimedia classes). A class CL_m in time slot k is characterized by the set of parameters $\psi_m^k = \{N_m^k, A_m^k, D_m^k, Q_m, depth_m^k\}$. These parameters are discussed next.

- 1) *Packet number*: Let N_m^k represent the number of packets in the transmission buffer of class CL_m in time slot k .
- 2) *Arrival rate and discard rate*: Let A_m^k denote the arrival rate, which represents the number of packets in class CL_m that arrive in time slot k . Let D_m^k denote the discard rate, which represents the number of packets in class CL_m whose delay deadline expires in time slot k . A packet is purged from the buffer if a) it is successfully transmitted or b) its delay deadline is expired. Based on the packet arrivals and departures, the number of packets N_m^k varies over time. In practice, if the multimedia data is pre-encoded, the arrival time t_m of the data units in each time slot can be computed *a priori*. Hence, the arrival rate A_m^k can be accurately modeled.
- 3) *Delay deadline*: We assume each class CL_m has a delay deadline d_m . The deadline is defined as the latest time that the packets need to be transmitted, or the packets cannot be decoded in time at the receiver (considering both the propagation delay, and playback delay at the receiver). Given the delay deadline, the discard rate can be written as $D_m^k = N_m^k I(kT \leq t_m + d_m \leq (k+1)T)$.
- 4) *Distortion impact*: We assume an additive distortion reduction for the packets similar to the one employed in [17] and [18]. Let the distortion reduction when the packets in class CL_m are received and decoded at the receiver be $N_m^k Q_m$, where Q_m represents the distortion impact of the class CL_m .
- 5) *Depth*: Some classes of packets need to be received before others. Such interdependencies among the multimedia classes can be represented using a DAG [17].

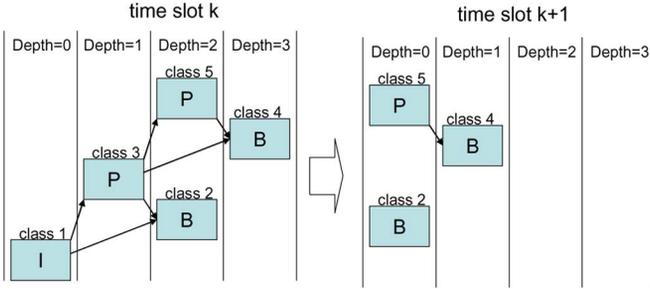


Fig. 1. Travelling tree example with MPEG IBPBP video frames.

Fig. 1 gives an example of a DAG, in which MPEG video frames are classified into classes. More examples can be found in [17] and [18], and our solution is not restricted to any packet classification methods. Based on the DAG, if there is a path from class CL_m to CL_n , we say the class CL_m is an ancestor of CL_n , and CL_n is a descendent of CL_m . Denote \mathbf{Anc}_m and \mathbf{Des}_m as the ancestor set and descendent set of the class CL_m . Let $depth_m^k$ represent the depth (the maximum distance) from class CL_m to the root in the DAG in time slot k . For classes at the root of the DAG, we define its depth to be 0. Depth captures the importance of a class in terms of interdependency, which depends on the depths of the ancestor classes, i.e., $depth_m = \max_{CL_n \in \mathbf{Anc}_m} depth_n + 1$. The DAG structure varies over time as a traveling tree in [18]. Fig. 1 also shows the variation of the DAG when the packets in class CL_1 and CL_3 are transmitted in time slot k .

Sophisticated packet classification can be performed in the application layer based on the different video coding structures. Based on the packet classification, the attributes $[q_m^k, m = 1, \dots, M]$ for each class are determined [18]–[20].

Let $\pi_m^k \in \{1, 0\}$ represent the transmission permission in class CL_m in time slot k . We assume that if $\pi_m^k = 1$, then all of the N_m^k packets of class CL_m are transmitted in time slot k ; if $\pi_m^k = 0$, then no packets in CL_m are transmitted. Denote $r_m^k(\pi_m^k) = N_m^k \pi_m^k l$ as the source rate of class CL_m in time slot k , and denote $\mathbf{r}^k = [r_m^k, m = 1, \dots, M]$ as the vector of rates for all the classes in time slot k . In addition, let $\pi_{APP}^k = [\pi_m^i, i = 1, \dots, k, m = 1, \dots, M]$ represent the transmission permissions of all the classes from time slot 1 to time slot k . Hence, the availability ρ_m^k of the class CL_m at the receiver in time slot k can be computed by $\rho_m^k(\pi_{APP}^k) = I(\sum_{i=1}^k \pi_m^i \geq 1)$, where $I(\cdot)$ represents an indicator function. Based on the DAG, the actual distortion reduction for a class depends on whether or not its ancestors are available at the receiver. Hence, the actual distortion reduction of class CL_m can be written as

$$Q_m^{act}(\pi_{APP}^k) = Q_m \prod_{CL_n \in \mathbf{Anc}_m} \rho_n^k(\pi_{APP}^k). \quad (1)$$

The resulting multimedia distortion reduction in time slot k can be represented by

$$\bar{Q}^k(\mathbf{r}^k(\pi_{APP}^k)) = \sum_{m=1}^M Q_m^{act}(\pi_{APP}^k) r_m^k(\pi_m^k). \quad (2)$$

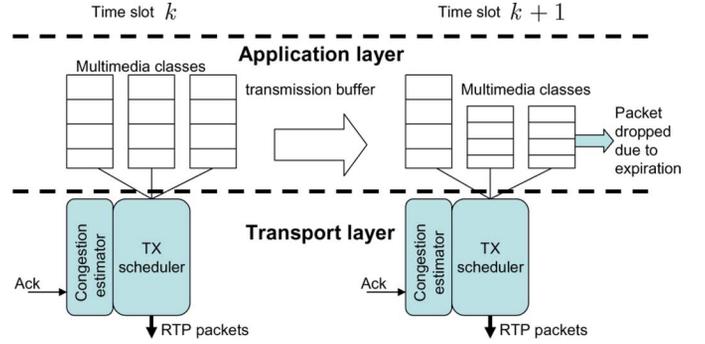


Fig. 2. System diagram of MTCC in time slot k and $k+1$.

C. Conventional Flow-Based Solutions

Most existing TCP-friendly congestion control solutions for multimedia streaming reactively adopt the available TCP throughput as a rate-budget constraint and maximize the immediate multimedia quality at the application layer (e.g., the rate-distortion optimization in [11] and the packet size adaptation in [7]). These solutions can be formulated using the following flow-based optimization.

1) Myopic-Flow-Based Optimization¹:

$$\begin{aligned} & \text{maximize}_{[\pi_m^k, m=1, \dots, M]} \bar{Q}^k([\pi_m^k, m = 1, \dots, M]) \\ & \text{s.t.} \sum_{m=1}^M r_m^k \leq R_{TCP}(Rtt, p^k). \end{aligned} \quad (3)$$

Note that these solutions passively adopt the available TCP throughput $R_{TCP}(Rtt, p^k)$ to consider the network condition p^k in each time slot. In contrast, we aim to propose a congestion control mechanism that adapts the congestion window size to both the network congestion and the specific characteristics and requirements of multimedia applications. Instead of shaping the traffic at the application layer to match the available throughput, the proposed MTCC jointly optimizes the congestion window size and the transmission permissions of classes at the transport layer to maximize the expected multimedia quality. In Section II-D, we discuss the MTCC congestion control problem in more details.

D. Proposed Packet-Based MTCC Solution

The proposed MTCC congestion control is illustrated in Fig. 2.

1) *At the Application Layer*: Multimedia RTP packets are classified into M classes based on their interdependencies. The packets of different classes are queued in different transmission (post-encoding) buffers for transmission.

2) *At the Transport Layer*: MTCC adopts the same error control as TCP, which retransmits the lost packets based on negative acknowledgements. However, unlike TCP which keeps retransmitting the lost packets until success, MTCC will drop all the expired packets in the transmission buffer (with unlimited buffer length, so that the packets are dropped only due to expiration). Moreover, unlike TCP that adopts an AIMD-based congestion

¹We assume that the information of actual distortion reduction $Q_m^{act}(\pi_{APP}^k)$ is available in both (3) and (6).

control, MTCC adjusts the congestion window size relying on the following two components:

3) *Transmission Scheduler*: The transmission scheduler selects the classes of packets to transmit and also determines the number of packets to be sent in time slot k . Specifically, the packet scheduler computes the priority metrics $\mathbf{x}^k = [PM_1^k, \dots, PM_M^k] \in \mathbb{R}^M$ for all the classes to capture the marginal benefit (in terms of decreasing the expected distortion) when the packets in class CL_m are transmitted in time slot k . In Section IV, we will discuss how to optimally determine these priority metrics PM_m^k based on the application attributes $[\psi_m^k, m = 1, \dots, M]$ and the network conditions. Based on the priority metrics, a simple transmission policy can be determined. For example, the transmission permission π_m^k for each class and the resulting congestion window size W^k can be determined as

$$\pi_m^k(\mathbf{x}^k) = I(PM_m^k > 0), W^k(\mathbf{x}^k) = \sum_{m=1}^M N_m^k \pi_m^k(\mathbf{x}^k). \quad (4)$$

4) *Network Estimator*: The network estimator updates the packet loss rate p^k and evaluates the network congestion metrics in each time slot as in TCP. For example, a simple updating rule of the packet loss rate can be written as [11]

$$p^{k+1}(p^k, W^k) = \alpha p^k + (1 - \alpha) \hat{p}^k(W^k) \quad (5)$$

where $\hat{p}^k(W^k)$ represents the realization of the packet loss rate in time slot k , and α represents the updating rates. In this paper, we focus on the joint optimization of the congestion window size and transmission scheduling by the transmission scheduler. For exposition simplicity, we assume that the only network congestion metric is the expected TCP window size $W_{TCP}^k(p^k)$. Note that other congestion metrics and more sophisticated updating rules (as in [4] and [11]) can be easily integrated into the proposed MTCC.

Note that MTCC only modifies the congestion window size adaptation in TCP. It is an end-to-end solution that does not rely on QoS functionality in routers, random early drop (RED), and other active queue management (AQM) [14]. Moreover, it does not require any modification at the receiver side as long as the sender signals the expired data sequence number. Hence, the receivers can operate as if they would receive regular TCP. However, MTCC can potentially benefit from the network level facilities, e.g., RED and AQM, which are areas of future work.

We assume that the proposed MTCC congestion control adheres to the following TCP-friendliness constraint.

Definition 1. Horizon- K TCP-Friendliness: A congestion control scheme is *horizon- K TCP-friendly*, if and only if the congestion control window sizes from current time slot i to time slot $i + K - 1$ satisfy the condition $\sum_{k=i}^{i+K-1} (W^k / W_{TCP}^k(p^k)) \leq K$.

The horizon- K TCP-friendliness constraint keeps the average TCP-friendliness ratio W^k / W_{TCP}^k close to 1 over the horizon K . Based on this definition, in current time slot i , the proposed MTCC congestion control solves the following packet-based optimization.

5) *Foresighted-Packet-Based Optimization*:

$$\begin{aligned} & \underset{\mathbf{x}^i \in \mathbb{R}^M}{\text{maximize}} \quad \sum_{k=i}^{i+K-1} \bar{Q}^k([\pi_m^k(\mathbf{x}^k), m = 1, \dots, M]) \\ & \text{s.t.} \quad \frac{1}{K} \sum_{k=i}^{i+K-1} \frac{W^k(\mathbf{x}^k)}{W_{TCP}^k(p^k)} \leq 1, \\ & \quad \quad 0 \leq W^k(\mathbf{x}^k) \leq W^{\max} \end{aligned} \quad (6)$$

where W^{\max} represents the maximum congestion window size.

Comparing our MTCC using the foresighted-packet-based optimization in (6) with the conventional solutions using the myopic-flow-based optimization in (3), the differences are:

- 1) Conventional solutions passively adapt the congestion window size to the network condition (e.g., the expected packet loss rate p^k). Our proposed MTCC solution takes one step further by adapting the congestion window size to the network conditions as well as to the application characteristics by optimizing the transmission scheduling. This allows the user to adapt the congestion window size to the characteristics of the multimedia packets in the buffer to provide differential services for various packet classes. Hence, a packet class with a higher distortion impact or more stringent delay deadline has a higher chance to be transmitted, which is desirable for maximizing the received multimedia quality.
- 2) MTCC maximizes the expected long-term distortion reduction over a horizon- K instead of solely maximizing the immediate distortion reduction as in the conventional solutions. This is especially important for multimedia applications with content dependencies. For example, in the IBPBP frame structure in Fig. 1, the MTCC user may want to plan the congestion window sizes for transmitting I and P frames, instead of myopically determining window sizes for the B frames.
- 3) Instead of performing a constrained rate optimization myopically at every time slot, MTCC adopts the horizon- K TCP-friendliness constraint. Note that the horizon- K TCP-friendliness becomes the traditional rate budget constraint in (3) when $K = 1$. The larger horizons provide long-term TCP-friendliness, which leads to more flexible window sizes and a better expected long-term quality. However, the short-term TCP-unfriendliness can be high and it needs to be compensated in the subsequent time slots [12].

In Section III, we discuss how the foresighted-packet-based optimization in (6) can be solved by applying an FHMDP framework.

III. FINITE-HORIZON MARKOV DECISION PROCESS

In this section, we first formulate the MTCC congestion control problem in (6) using an FHMDP with Markovian state transition. The complexity of the FHMDP can be high due to the large state space. Hence, in Section IV, we will decompose the problem into simpler sub-problems having smaller state spaces. We model this problem as an FHMDP due to the following reasons:

- 1) In numerous multimedia applications, multimedia traffic can be described by Markov models (as in [24]).
- 2) TCP operations are commonly modeled by discrete-time finite-state Markov chains (see, e.g., [2], [5], [15]). Hence, the average TCP window size can be described by Markovian models based on the states of all the users (or the aggregate states as in [9]) in the network.

The FHMDP framework can be defined by the tuple $\{\mathcal{A}, \mathcal{S}, P, u, \gamma, \lambda, K\}$. The various components of the framework are described next:

- 1) *Action*: We denote the action of the FHMDP in time slot k as $a^k = [\pi_m^k, m = 1, \dots, M] \in \mathcal{A} = \{0, 1\}^M$.
- 2) *State and State Transition*: We denote the state of the FHMDP in time slot k as $s^k = \{W_{TCP}^k, \mathbf{N}^k\} \in \mathcal{S}^{Net} \times \mathcal{S}^{App} = \mathcal{S}$, where the expected TCP window size W_{TCP}^k represents the network state and the number of packets $\mathbf{N}^k = [N_m^k, m = 1, \dots, M]$ in all the packet classes represents the application state. Let $\mathcal{S}^{Net} = \{0, \dots, W^{\max}\}$ represent the state space of the network state W_{TCP}^k , and let $\mathcal{S}^{App} = \{0, \dots, N^{\max}\}^M$ represent the state space of the application state, where W^{\max} represents the maximum number of the window size and N^{\max} represents the maximum number of packets in a class. Let $P : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow [0, 1]$ denote the state transition function, which can be described for the network state and application state as follows:
 - a) The network state transition is described by the state transition probabilities $P(W_{TCP}^{k+1}|W_{TCP}^k)$, which can be evaluated by estimating the next possible packet loss rate p^{k+1} given the current feedback p^k as in [9] and [15]. In general, the number of TCP users in the network is large enough such that the network state transition is not impacted by a single user's action.
 - b) The application state transition is described by the state transition probabilities $P(\mathbf{N}^{k+1}|\mathbf{N}^k, a^k)$. The number of packets in each class varies over time depending on the action a^k . Note that each class can have its own arrival rate per time slot $A_m^k \geq 0$ and its own discard rate per time slot $D_m^k \geq 0$. Therefore, the application state transition can be computed as

$$\begin{aligned} N_m^{k+1} &= N_m^k(1 - \pi_m^k) + A_m^k - D_m^k(1 - \pi_m^k) \\ &= \underbrace{(N_m^k - D_m^k)(1 - \pi_m^k)}_{\text{remaining number of packets after packet departure}} + \underbrace{A_m^k}_{\text{packet arrivals}}. \end{aligned} \quad (7)$$

This framework can be applied to both pre-encoded and real-time multimedia applications. For pre-encoded multimedia applications, the MTCC user knows the state transitions for the entire multimedia session and solves the finite-horizon dynamic programming problem. For real-time multimedia applications, MTCC can apply stochastic models to capture the state transitions of the applications [18].

Since the network state transition and the application state transition are independent, we define the overall state transition probabilities² as: $P(s^{k+1}|s^k, a^k) = P(W_{TCP}^{k+1}|W_{TCP}^k)P(\mathbf{N}^{k+1}|\mathbf{N}^k, a^k)$.

- 3) *Utility, Discount Factor, and Horizon Definitions*: First, we apply a positive Lagrangian multiplier λ and modify (6) into an unconstrained optimization:

$$\begin{aligned} &\text{maximize}_{a^i \in \mathcal{A}} \sum_{k=i}^{i+K-1} \bar{Q}^k(a^k, s^k) \\ &\quad - \lambda \left(\sum_{k=i}^{i+K-1} \frac{W^k}{W_{TCP}^k} - \sum_{k=i}^{i+K-1} 1 \right) \\ &= \text{maximize}_{a^i \in \mathcal{A}} \sum_{k=i}^{i+K-1} u^k(a^k, s^k) \end{aligned} \quad (8)$$

where $u^k(a^k, s^k) = \bar{Q}^k(a^k, s^k) - \lambda(W^k/W_{TCP}^k - 1)$ is referred to as the *instantaneous utility* in time slot k . The second term of the instantaneous utility can be interpreted as the TCP window size deviation cost. The Lagrangian multiplier λ determines how the MTCC user favors the TCP-friendliness over the multimedia quality. Based on the unconstrained optimization, the objective of the FHMDP in time slot i is defined as

$$\chi^i(s^i) = \arg \max_{a \in \mathcal{A}} \sum_{k=i}^{i+K-1} \gamma^{k-i} u^k(s^k, a^k) \quad (9)$$

where $\chi^i(s^i)$ represents the optimal congestion control policy given the state s^i at the time slot i , and γ represents the discount factor ($0 \leq \gamma \leq 1$). Note that (9) is equivalent to the unconstrained optimization in (8) when $\gamma = 1$. Since the Markovian models of the network state and application state transition may not be accurate, the discount factor γ is set smaller than 1 to alleviate the impact of the inaccurate future utilities. The tradeoff between the TCP-friendliness and multimedia quality with different λ and γ will be discussed in Section VI.

Note that the MTCC not only maximizes the instantaneous utility, but also the expected future utilities, which are expressed using the expected utility-to-go, which is defined next.

Definition 2. Expected Utility-to-go³: Define the expected utility-to-go at the last time slot of the horizon as $J_\mu^{i+K-1}(s) = u^{i+K-1}(s, \mu(s))$, $\forall s \in \mathcal{S}$, where $\mu : \mathcal{S} \rightarrow \mathcal{A}$ represents a stationary mapping from the given state to an action. We define the expected utility-to-go in time slot $k = i, \dots, i + K - 2$ as

$$\begin{aligned} J_\mu^k(s^k) &= u^k(s^k, \mu(s^k)) \\ &\quad + \gamma \sum_{s^{k+1} \in \mathcal{S}} P(s^{k+1}|s^k, \mu(s^k)) J_\mu^{k+1}(s^{k+1}). \end{aligned}$$

²In this work, we assume that the state transition probabilities can be calculated a priori. In fact, the state transition probabilities can be learned on the fly as long as the transitions of the states are semi-stationary.

³RTT may not be constant, but as long as it has comparably small variation within the horizon, the expected utility-to-go can be relatively accurate with the new RTT value.

$\pi_m^{i*}(s^i) = I(PM_m^{i*}(s^i) > 0)$, where the optimal priority metric $PM_m^{i*}(s^i)$ is computed by

$$PM_m^{i*}(s^i) = \left(Q_m - \frac{\lambda}{W_{TCP}^i} \right) N_m^i + \gamma \sum_{s^{i+1} \in \mathcal{S}} P(W_{TCP}^{i+1} | W_{TCP}^i) \times \left(\begin{array}{c} J_{\mu,m}^{i+1}(W_{TCP}^{i+1}, N_m^{A,i}) \\ - J_{\mu,m}^{i+1}(W_{TCP}^i, N_m^i - (N_m^{D,i} - N_m^{A,i})) \end{array} \right). \quad (12)$$

Proof: See Appendix C.

Theorem 2 indicates that when the packets are coded independently, the MTCC congestion control problem becomes an optimal stopping problem [23], where the MTCC user transmits the packets of a certain class if and only if the priority metric of the class is positive. The priority metrics $\mathbf{x}^{i*}(s^i) = [PM_m^{i*}(s^i), m = 1, \dots, M]$ quantify the benefits of transmitting packets from various classes as opposed to not transmitting them in time slot i . Importantly, in addition to the distortion impact Q_m , the MTCC user needs to consider the arrival rates and discard rates of the various classes. If a class CL_m has numerous expiring packets (i.e., $D_m^i - A_m^i$ is large), it can be shown that the respective class has a larger $PM_m^{i*}(s^i)$ to be transmitted in time slot i , instead of waiting for a future time slot. Moreover, it can be shown that at a time slot with a better network state (larger W_{TCP}^i), we have larger priority metrics from (12) for all the classes and hence, more classes are able to obtain the transmission permissions. Based on Theorem 2, we have the following remarks:

Remark 3: In (12), as γ approaches 0, the user prefers to prioritize the packet classes based on their distortion impact values Q_m . As γ approaches 1, the user increasingly weights the impact from the arrival rate and discard rate on the future expected utility. Note that when $\gamma = 0$, the FHMDP problem in (9) becomes a myopic optimization that merely optimizes the instantaneous utility, which is equivalent to solving an unconstrained optimization of the conventional solution in (3).

Remark 4: Note that the optimal congestion control policy $\chi^i(s^i)$ in (9) includes the optimal priority metrics $\mathbf{x}^{i*}(s^i)$ and the congestion window size $W^{i*}(s^i)$. Theorem 2 provides the optimal priority metrics $\mathbf{x}^{i*}(s^i) = [PM_m^{i*}(s^i), m = 1, \dots, M]$. Based on this, the optimal congestion window size $W^{i*}(s^i)$ of the MTCC user can be written as $W^{i*}(s^i) = \sum_{m=1}^M N_m^i I(PM_m^{i*}(s^i) > 0)$ and the resulting expected multimedia quality can be computed by $\bar{Q}^i(s^i) = \sum_{m=1}^M Q_m N_m^i I(PM_m^{i*}(s^i) > 0)$. Note that the optimal policy varies with both the application state and the network state in time slot i ($s^i = \{W_{TCP}^i, \mathbf{N}^i\}$).

In Appendix A, Algorithm 1 provides the specific procedures for computing the optimal congestion policy $\chi^i(s^i)$ when the packets are independent. The time complexity of the algorithm is $O(KM(W^{\max} N^{\max})^2)$.

B. Decomposition With Interdependently Coded Packets

In this subsection, we investigate the decomposition of the FHMDP problem when the packets have interdependencies,

described by a DAG as introduced in Section II-A. The following theorem presents the structural results of solving the FHMDP problem.

Theorem 3. Structural Results of MTCC With Interdependent Packets: Given the DAG and the state s^i in time slot i , the FHMDP problem can be solved by repeating the following two phases:

Phase 1. Select packet classes to transmit at the current time slot at the depth $depth_n^i = j - 1$:

$$\pi_m^{i*}(s^i) = I(PM_m^{i*}(s^i) > 0) \\ \forall CL_m \in \{CL_n, depth_n^i = j - 1\}$$

where

$$PM_m^{i*}(s^i) = \left(Q_m^{act} - \frac{\lambda}{W_{TCP}^i} \right) N_m^i + \gamma \sum_{s^{i+1} \in \mathcal{S}} P(W_{TCP}^{i+1} | W_{TCP}^i) \times \left(\begin{array}{c} J_{\mu,m}^{i+1}(W_{TCP}^{i+1}, N_m^{A,i}) - \\ J_{\mu,m}^{i+1}(W_{TCP}^i, N_m^i - (N_m^{D,i} - N_m^{A,i})) \end{array} \right) \quad (13)$$

and j represents the number of iterations.

Phase 2. Update the actual distortion impact of each class: $Q_m^{act} = Q_m \prod_{\forall CL_n \in \text{Anc}_m^i} \pi_n^{i*}$, $m = 1, \dots, M$.

Proof: Considering the DAG structure, the packets only depend on the other packets that have smaller depths, i.e., Theorem 2 is applicable for the packets in a specific depth j , given the transmission policy of the packets in depth $i < j$. The impact of the transmission policy of the packets in the smaller depth can be entirely captured by the actual distortion impact Q_m^{act} .

In Phase 1, the MTCC user selects packet classes for transmission by applying Theorem 3 starting from the classes at the root of the DAG. Since classes with the same depth are independent of each other, Theorem 2 can be applied to Phase 1 for classes with the same depth. Phase 2 indicates that if a class has no transmission permission, i.e., $\pi_m^{i*}(s^i) = 0$, the MTCC user set all its descendants' distortion impact to 0, i.e., Q_n^{act} for $\forall CL_n \in \text{Des}_m$ (see Section II-B). Based on the DAG, since the distortion impact of a class is only influenced by the ancestors, the greedy algorithm in Theorem 3 starting from the root provides the optimal congestion policy. The two phases are repeated until the maximum depth of the DAG is reached.

In Appendix A, Algorithm 2 provides the procedures for computing the optimal congestion control policy $\chi^i(s^i) = \{\mathbf{x}^{i*}(s^i), W^{i*}(s^i)\}$ when the packets are interdependently coded. Assuming that the DAG has the maximum depth \bar{D} and the number of classes per depth is \bar{M} on average, the complexity of the algorithm can be represented by $O(\bar{M}\bar{D}K(W^{\max} N^{\max})^2)$.

V. FAIRNESS AMONG MULTIPLE MTCC STREAMS

In the previous sections, we focus on only one MTCC user interacting with multiple regular TCP users in the same network. In this section, we assume that there are V MTCC

users interacting with other TCP users in a network and investigate the competition among the multimedia users. Denote $\mathbf{V} = \{V_n, n = 1, \dots, V\}$ as the set of the MTCC users. Denote user V_n 's expected multimedia distortion reduction in time slot k as \bar{Q}_n^k . We assume a saturated condition (i.e., all the users continuously have their source traffic fed into their transmission buffers). We apply the well-known Jain's fairness index [26] to quantify the fairness among the V MTCC users. Unlike other TCP research that applies Jain's fairness index over throughput, here we focus on the fairness among multimedia qualities, i.e., the index becomes

$$\mathcal{F}^k = \frac{\left(\sum_{n=1}^V \bar{Q}_n^k\right)^2}{V \sum_{n=1}^V (\bar{Q}_n^k)^2}. \quad (14)$$

The fairness index \mathcal{F}^k measures the quality deviation of the multimedia applications. It varies as the MTCC users make their own decisions at each time slot. Note that the index is always bounded by 1. The quality-based fairness is reached, i.e., $\mathcal{F} = 1$, only when all the MTCC users have the same multimedia quality.

Following the TCP response function introduced in Section II-B and the packet loss rate updating rules in Section II-D, the expected network state of a user V_n in the next time slot can be expressed as $E[W_{TCP,n}^{k+1}(p_n^k, W_n^k)] = \sqrt{1.5/p_n^{k+1}(p_n^k, W_n^k)}$. Similarly, we denote $E[PM_{mn}^{k+1}]$ as the expected priority metric of CL_m (the m th class of user V_n) in time slot $k+1$, which can be shown as a function of W_n^k . Then, we can prove the following lemma.

Lemma 1: For user V_n , its priority metrics $\{E[PM_{mn}^{k+1}(W_n^k)], \forall CL_{mn} \in V_n\}$ are all nonincreasing functions of W_n^k , if

- 1) $\gamma = 0$, or
- 2) $0 < \gamma \leq 1$, $N_m^{D,k} = N_m^k, \forall CL_{mn} \in V_n, k = 1, \dots, K$.

Proof: For both conditions, the priority metric of class CL_{mn} can be written by $E[PM_{mn}^{k+1}(W_n^k)] = Q_{mn} - \lambda/E[W_{TCP,n}^{k+1}(p_n^k, W_n^k)]$ based on (12). Since the estimated packet loss rate $p^{k+1}(p^k, W^k)$ is in general a monotonically nondecreasing function of the congestion window size W_n^k [11], it is straightforward that both the expected window size $E[W_{TCP,n}^{k+1}(p_n^k, W_n^k)]$ and the expected priority metrics $E[PM_{mn}^{k+1}(W_n^k)]$ in the next time slot are nonincreasing functions of W_n^k . ■

Lemma 1 indicates that the priority metrics $E[PM_{mn}^{k+1}(W_n^k)], \forall CL_{mn} \in V_n$ are nonincreasing functions of W_n^k when the users apply the myopic MTCC or when the packets in the buffer expire in the next time slot. In these two cases, the priority metrics are dominated by the first term in (12). The second condition requires the delay deadlines of the classes to be stringent, which is more likely to be true in the case of real-time streaming, as opposed to the pre-encoded streaming applications. In these two cases, Lemma 1 indicates that the competition among users makes it impossible for a user to excessively increase its congestion window size in order to improve its own quality. The increase of the congestion window size W_n^k may decrease the priority metrics and hence, reduce the resulting distortion reduction in the next time slot. Following Remark 4 in Section IV, the multimedia distortion

reduction of user V_n in the next time slot can be written as

$$\bar{Q}_n^{k+1}(W_n^k) = \sum_{\forall CL_{mn} \in V_n} Q_{mn} N_{mn} \times I(E[PM_{mn}^{k+1}(W_n^k)] > 0) \quad (15)$$

where Q_{mn} represents the distortion impact of class CL_{mn} . Comparing $\bar{Q}_n^{k+1}(W_n^k)$ with the current multimedia distortion reduction \bar{Q}_n^k , the variation appears only for the classes whose priority metrics change sign. If we denote \mathbf{M}_n^k as the set of classes whose priority metrics follow $PM_{mn}^k E[PM_{mn}^{k+1}] < 0$, we can rewrite (15) as

$$\bar{Q}_n^{k+1} = \begin{cases} \bar{Q}_n^k, & \text{if } \mathbf{M}_n^k = \emptyset \\ \bar{Q}_n^k + \Delta\bar{Q}_n^k, & \text{if } PM_{mn}^k < E[PM_{mn}^{k+1}], \\ & \forall CL_{mn} \in \mathbf{M}_n^k \\ \bar{Q}_n^k - \Delta\bar{Q}_n^k, & \text{if } PM_{mn}^k > E[PM_{mn}^{k+1}], \\ & \forall CL_{mn} \in \mathbf{M}_n^k \end{cases} \quad (16)$$

where $\Delta\bar{Q}_n^k = |\bar{Q}_n^{k+1} - \bar{Q}_n^k| = \sum_{\forall CL_{mn} \in \mathbf{M}_n^k} Q_{mn} N_{mn} \geq 0$ represents the difference of the expected distortion reduction of user V_n in time slot k . Based on (16), we next prove the sufficient condition for achieving the discussed quality-based fairness.

Lemma 2: The difference of the fairness index is nonnegative, i.e., $\Delta\mathcal{F}^k = \mathcal{F}^{k+1} - \mathcal{F}^k \geq 0$, if

$$\sum_{V_n \in \mathbf{V}} (\bar{Q}_n^k)^2 \sum_{V_n \in \mathbf{V}} \Delta\bar{Q}_n^k \geq \sum_{V_n \in \mathbf{V}} \bar{Q}_n^k \sum_{V_n \in \mathbf{V}} \bar{Q}_n^k \Delta\bar{Q}_n^k. \quad (17)$$

Proof: We omit the proof here due to space limitations. A similar proof can be found in [16].

Lemma 2 provides a sufficient condition that ensures a non-decreasing fairness index $\Delta\mathcal{F}^k$. Since the index is bounded by 1, the interaction among users asymptotically drives the fairness index to 1 [16]. Based on Lemma 2, the following theorem provides the sufficient conditions for multiple myopic MTCC users to reach the quality-based fairness.

Theorem 4: The fairness index of multiple MTCC users $V_n \in \mathbf{V}$ converges to 1, i.e., $\mathcal{F}^\infty = 1$, if the following sufficient conditions are satisfied:

- 1) $Q_{mn} = Q_{mn'} = Q_m, \forall V_n, V_{n'} \in \mathbf{V}$
- 2) $N_{mn} \geq N_{m'n'}$ for any $Q_m \geq Q_{m'}, \forall V_n, V_{n'} \in \mathbf{V}$.
- 3) $E[PM_{mn}^{k+1}(W_n^k)], \forall CL_{mn} \in V_n, \forall V_n \in \mathbf{V}$ are all non-increasing functions of W_n^k using the same λ .

Proof: See Appendix D.

The first condition in Theorem 4 indicates that the MTCC users apply the same set of $[Q_m, m = 1, \dots, M]$ to classify their M classes of the multimedia applications. The second condition indicates that for all the users in the network, users have more packets in a class with higher distortion impact than a class with lower distortion impact. This condition can be realized in many video coding techniques with appropriate classification. For example, in MPEG video frames, I-frames usually contain much more information bits than P-frames and B-frames. The third condition is discussed in Lemma 1. Based on (16), as long as the priority metrics $E[PM_{mn}^{k+1}(W_n^k)]$ are nonincreasing functions of W_n^k for all the classes, we can show that a user with a larger multimedia quality \bar{Q}_n will always have a smaller quality change $\Delta\bar{Q}_n$ when users applying MTCC to change their congestion window size. In Appendix D, we prove that this allows the proposed MTCC to satisfy the sufficient condition in Lemma

TABLE II
CLASSIFICATION OF THE SEQUENCES

Class CL_m	1	2	3	4	5~8	9~16
Q_m (dB/pkt) range	0.154	0.153	0.09	0.08	~ 0.07 2	~ 0.05 3
N_m^0 of “Coastguard” per GOP	17	17	12	12	5	4
N_m^0 of “Foreman” per GOP	34	34	8	8	4	0
N_m^0 of “Mobile” per GOP	30	30	13	13	1	0

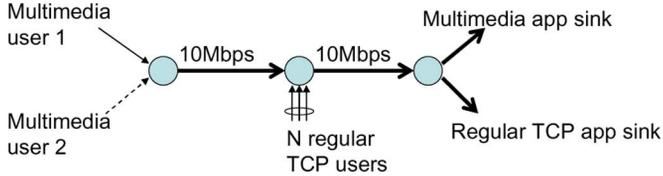


Fig. 4. Simulation settings.

2 and hence the quality-based fairness index converges to 1. Finally, the three conditions in Theorem 4 lead to $\mathcal{F}^\infty = 1$ for MTCC users $V_n \in \mathcal{V}$.

VI. SIMULATION RESULTS

In this section, we simulate the proposed congestion control scheme using different video sequences: “Foreman”, “Mobile”, and “Coastguard” (at a frame rate of 30 Hz, CIF format). The sequences are encoded using an embedded scalable video codec [31] at the bitrate of 1500 Kbps. To perform the RD adaptation we use the multitrack hinting developed in [31], which provides the possibility for different coding methods and diverse elementary bitstream syntax structures to be supported by the same server in a common fashion, independent of server design and implementation. Given a certain multitrack-hint specification, packet scheduling is concerned with the following: 1) the establishment of which packets out of which layers should be transmitted and the protection mechanism corresponding to the expected error rate and 2) the establishment of each packet’s departure time. How to implement such packet scheduling algorithms for a given codec is also discussed in detail in [31] and used in this paper for our video streaming illustrations. The proposed methodology is applicable for any video codec, but in this paper, like in [31], we used for illustration a motion compensated temporal-filtering (MCTF)-based scalable codec called SIV, which was introduced in [32]. We assume that each group of picture (GOP) contains 16 frames and each of them can tolerate a playback delay of $\{133, 266, 400, 533\}$ ms. We set the packet length up to 1000 bytes and the video packets are classified into 16 classes based on their spatial and temporal interdependencies as in [19] and [20]. Table II provides a summary of the classifications of the sequences. We simulate the video transmission using MATLAB using the simulation settings in Fig. 4. There are 20 regular TCP users and the resulting average RTT for the video packets is 133 ms.

A. Tradeoff Between Multimedia Performance and TCP Friendliness

First, we simulate the case without the MTCC user 2. We focus on the MTCC user 1 streaming the “Coastguard” sequence

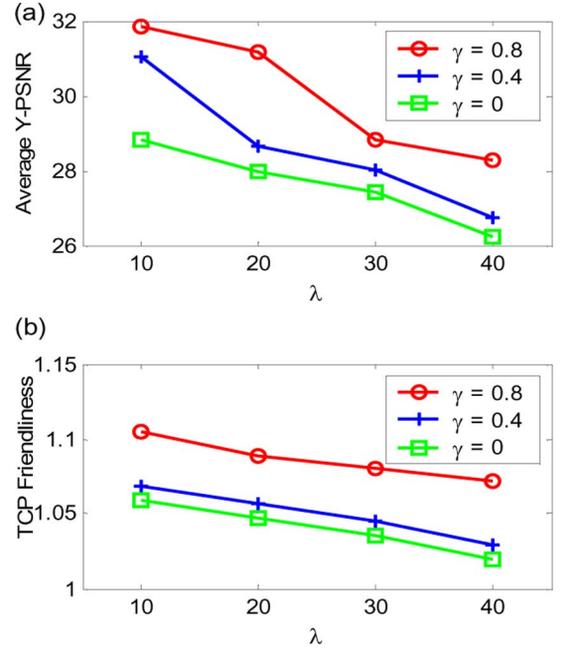


Fig. 5. (a) Average Y-PSNR of “Coastguard” sequence, (b) resulting TCP-friendliness versus different Lagrangian multipliers (playback delay: 266 ms, $K = 4$ RTT).

using the proposed MTCC congestion control with different Lagrangian multipliers and discount factors. Based on the measured packet loss rate, the MTCC user applies a Markov chain model (similar to the model applied in [9]) on the network states with an expected TCP window size $W_{TCP}^k = 16$ per RTT, and the horizon $K = 4$ RTT. Fig. 5 shows the tradeoff between multimedia quality and the horizon- K TCP-friendliness. Larger λ provides better TCP-friendliness, but achieves lower multimedia quality, because the quality gain is weighed less than the cost within the instantaneous utility. The results also show that the foresighted approach with larger γ significantly improves the multimedia quality while maintaining moderate TCP-friendliness. However, in this paper, we focus on deriving the optimal solution when the environment (i.e., the state transition probabilities) and the utility are perfectly known. If the transition probabilities are not perfect, a larger γ can lead to a worse learning performance. The selection of λ and γ for MTCC using online learning for the case when the environment is unknown represents an interesting future research direction.

B. Comparisons Against Alternative Congestion Control Solutions for Multimedia Applications

We simulate separately the streaming of “Coastguard” sequence as well as “Foreman” sequence using three different approaches: 1) our proposed packet-based MTCC congestion control (MT) that jointly optimizes the transmission scheduling and congestion window size; 2) a flow-based rate-distortion optimization approach (RD) [11] to optimize the transmission scheduling by adapting the sending rate to the available TFRC TCP throughput; 3) passive multimedia transmission directly over TCP connections (PA) as in [5].

Fig. 6 shows the average video quality of various approaches using different playback delays and clearly demonstrates that the joint transmission scheduling and congestion control optimization is essential for real-time multimedia transmission. Our

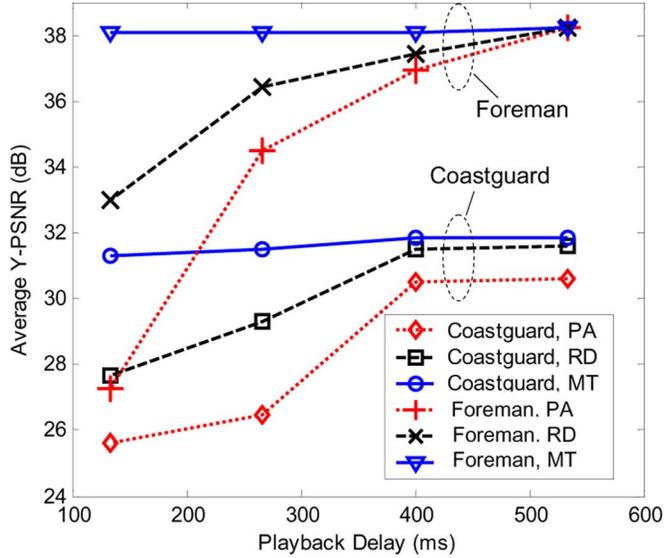


Fig. 6. Average received video quality using different TCP congestion control for multimedia transmission (for MT approach, $\lambda = 10$, $\gamma = 0.8$, $K = 4$ RTT).

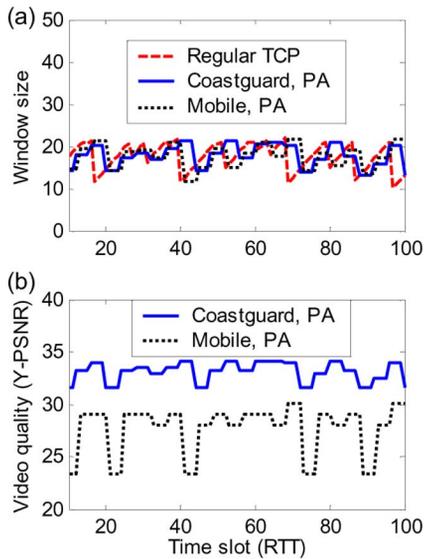


Fig. 7. (a) Congestion window sizes over time for the two multimedia users and the average congestion window size of the 20 regular TCP users. (b) Video quality over time for the two multimedia users using PA approach (playback delay: 533 ms).

proposed approach significantly outperforms the others especially when the playback delay is smaller than 400 ms (which is common in numerous real-time video streaming and videoconferencing applications), because it is able to jointly optimize the congestion window size as well as the transmission scheduling by considering the distortion impacts, delay deadlines, and interdependencies of the packets.

C. Fairness Among Multiple MTCC Streams

In this subsection, we validate the quality-based fairness among multiple users using MTCC. We simulate the case when multimedia user 1 streams “Coastguard” sequence and multimedia user 2 streams “Mobile” sequence simultaneously using the same simulation settings in Fig. 4 with 20 regular TCP users. The playback delay is set as 533 ms. Fig. 7 shows

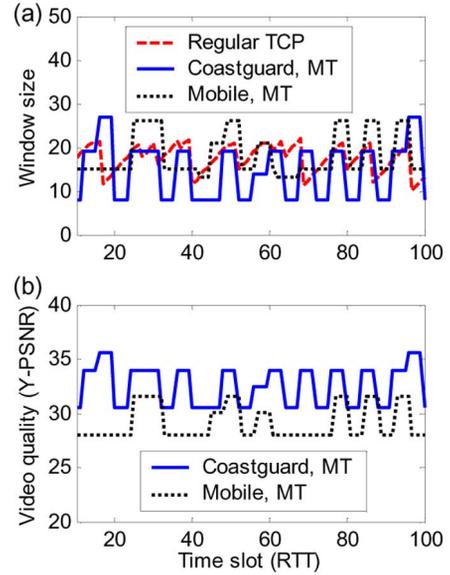


Fig. 8. (a) Congestion window sizes over time for the two multimedia users and the average congestion window size of the 20 regular TCP users. (b) Video quality over time for the two multimedia users using MT approach ($\lambda = 10$, $\gamma = 0.1$, $K = 4$ RTT, playback delay: 533 ms).

TABLE III
COMPARISONS OF THE VIDEO QUALITIES USING THE PA APPROACH AND THE PROPOSED MT APPROACH WHEN THE NUMBER OF USERS IN THE NETWORK INCREASES

(playback delay: 533ms)	PA approach				MT approach ($\lambda = 10$, $\gamma = 0.1$, $K = 4$ RTT)			
	Avg. PSNR of user 1 (dB)	Avg. PSNR of user 2 (dB)	Avg. PSNR of the users (dB)	Avg. window size of TCP users	Avg. PSNR of user 1 (dB)	Avg. PSNR of user 2 (dB)	Avg. PSNR of the users (dB)	Avg. window size of TCP users
N = 20	32.07	27.46	29.76	17.00	32.58	30.43	31.50	16.95
N = 25	31.14	25.61	28.37	14.14	31.43	30.40	30.91	13.80
N = 30	29.88	23.38	26.63	11.70	30.29	30.22	30.25	11.51

the congestion window size and the video quality over time when the multimedia users apply the passive multimedia transmission approach (PA) directly over TCP connections as in [5]. It is shown that although the congestion window sizes of the multimedia users follow the average TCP window size of the 20 regular TCP users, the video quality gap between the two sequences is always larger than 3 dB.

On the other hand, Fig. 8 shows the congestion window size and the video quality over time when the multimedia users apply the proposed MTCC congestion control (MT) algorithms. We classify the video packets of both sequences to satisfy the first two sufficient conditions in Theorem 4. We also set a small discount factor $\gamma = 0.1$ to ensure that the priority metrics $E[PM_{mn}^{k+1}(W_n^k)]$ are nonincreasing functions of W_n^k for all the classes. It is shown that MTCC results in closer streaming qualities for the two multimedia users at the cost of moderate TCP unfriendliness. Hence, by applying the proposed MTCC, the multimedia users fairly share the resources in terms of video quality. Moreover, by jointly optimize the transmission policy of the video classes, the proposed solution not only improves the

overall receiving video qualities, but also reduces the overall quality fluctuation experience by providing a certain minimal quality level and avoiding abrupt quality degradation.

We further increase the number of the regular TCP users using the same simulation settings. The resulting congestion window sizes and the video qualities are summarized in Table III. It is shown that the proposed MTCC congestion control is able to maintain the streaming qualities for both sequences as the number of users in the network increases, while having limited impact on the other regular TCP users. This is because the MTCC is able to better utilize the resource by prioritizing the video classes for transmission, in addition to merely adapting the congestion window size.

VII. CONCLUSIONS

In this paper, we formulate a media-aware congestion control for multimedia transmission using FHMDP that explicitly considers the distortion impacts, delay deadlines, and interdependencies of the various multimedia classes. The proposed approach not only adapts the congestion window size given the measured packet loss rate, but also optimally prioritizes the multimedia classes for transmission and, hence, further improves the multimedia quality. We show that this complex FHMDP problem can be decomposed into simpler optimal stopping problems, thereby significantly reducing the complexity of solving the problem. The simulation results show that the proposed foresighted MTCC significantly outperforms the conventional TCP-friendly congestion control schemes in terms of quality, especially for real-time streaming with a small playback delay. Moreover, unlike the conventional congestion control approaches focusing on the throughput-based fairness, our solution maintains the quality-based fairness among the multimedia users, which improves the overall streaming quality by utilizing the available bandwidth resources more efficiently.

APPENDIX A

Algorithm 1: MTCC congestion control with independent packets

For time slot $k = i$, given the current state s^i, λ, γ, K

Set $k = i + K - 1$;

While $k \geq i$

For all classes CL_m

Compute all $J_m^k(W_{TCP}^k, N_m^k)$ from (19),

for $N_m^k \in \{0, \dots, N_m^{\max}\}, W_{TCP}^k \in$

$\{0, \dots, W_{TCP}^{\max}\}$

Compute $PM_m^{k*}(s^k)$ and $\pi_m^{k*}(s^k)$ in (12);

End for

Set $k = k - 1$;

End while

Set $PM_m^{i*} = PM_m^{k*}(s^i)$ for $m = 1, \dots, M$;

Set $W^{i*} = \sum_{\forall m, PM_m^{i*} \geq 0} N_m^i$;

Algorithm 2: MTCC congestion control with interdependent packets

For time slot $k = i$, given the current state s^i, λ, γ, K

Set $k = i + K - 1$;

While $k \geq i$

Set $W^k = 0$ and $depth = 0$;

For all classes CL_m with $depth_m^k = depth$

Compute all $J_m^k(W_{TCP}^k, N_m^k)$ from (19),

for $N_m^k \in \{0, \dots, N_m^{\max}\}, W_{TCP}^k \in$

$\{0, \dots, W_{TCP}^{\max}\}$

Compute $PM_m^{k*}(s^k)$ and $\pi_m^{k*}(s^k)$ in (13);

If $PM_m^{k*}(s^k) < 0$, set $Q_n = 0$ for $\forall CL_n \in \text{Des}_m$;

Set $depth = depth + 1$;

End for

Set $k = k - 1$;

End while

Set $PM_m^{i*} = PM_m^{k*}(s^i)$ for $m = 1, \dots, M$;

Set $W^{i*} = \sum_{\forall m, PM_m^{i*} \geq 0} N_m^i$;

APPENDIX B

Proof of Theorem 1: Without losing generality, we assume $i = 1$. Since packets are independent, the distortion reduction $\bar{Q}^k(a^k, s^k)$ in (8) can be computed by $\bar{Q}^k(a^k, s^k) = \sum_{m=1}^M Q_m N_m^k \pi_m^k$. First, we see that when $k = K$, $J_\mu^K(s^K)$ can be rewritten as

$$\begin{aligned} & \sum_{m=1}^M Q_m N_m^K \pi_{\mu,m}^K - \frac{\lambda}{W_{TCP}^K} \left(\sum_{m=1}^M N_m^K \pi_{\mu,m}^K - W_{TCP}^K \right) \\ &= \sum_{m=1}^M \left(Q_m - \frac{\lambda}{W_{TCP}^K} \right) N_m^K \pi_{\mu,m}^K + C(W_{TCP}^K) \end{aligned} \quad (18)$$

where $[\pi_{\mu,m}^K, m = 1, \dots, M] = \mu(s^K)$ denotes the vector of transmission permissions given the policy $\mu(s^K)$. Based on this, the expected utility-to-go $J_\mu^K(s^K) = \sum_{m=1}^M (Q_m - \lambda/W_{TCP}^K) N_m^K \pi_{\mu,m}^K + \lambda M/W_{TCP}^K$ is separable and also a nondecreasing function of N_m^K . Then, by assuming $J_\mu^{k+1}(s^{k+1}) = \sum_{m=1}^M J_{\mu,m}^{k+1}(W_{TCP}^{k+1}, N_m^{k+1}) + C^{k+1}(W_{TCP}^{k+1})$

and assume $J_{\mu,m}^{k+1}(W_{TCP}^{k+1}, N_m^{k+1})$ are nondecreasing functions of N_m^{k+1} for all classes, we have

$$\begin{aligned} J_{\mu}^k(s^k) &= u^k(s^k, \mu(s^k)) + \gamma \sum_{s^{k+1} \in \mathcal{S}} P(s^{k+1}|s^k) J_{\mu}^{k+1}(s^{k+1}) \\ &= \sum_{m=1}^M \left(Q_m - \frac{\lambda}{W_{TCP}^k} \right) N_m^k \pi_{\mu,m}^k + \frac{\lambda}{W_{TCP}^k} \\ &\quad + \gamma \sum_{s^{k+1} \in \mathcal{S}} P(W_{TCP}^{k+1}|W_{TCP}^k) \\ &\quad \times \left(\sum_{m=1}^M J_{\mu,m}^{k+1}(W_{TCP}^{k+1}, N_m^{k+1}(\pi_{\mu,m}^k)) \right. \\ &\quad \left. + C^{k+1}(W_{TCP}^{k+1}) \right) \\ &= \sum_{m=1}^M J_m^k(W_{TCP}^k, N_m^k) + C^k(W_{TCP}^k) \end{aligned}$$

where

$$\begin{aligned} J_{\mu,m}^k(W_{TCP}^k, N_m^k) &= \left(Q_m - \frac{\lambda}{W_{TCP}^k} \right) N_m^k \pi_{\mu,m}^k \\ &\quad + \gamma \sum_{s^{k+1} \in \mathcal{S}} P(W_{TCP}^{k+1}|W_{TCP}^k) \\ &\quad \times J_{\mu,m}^{k+1}(W_{TCP}^{k+1}, N_m^{k+1}(\pi_{\mu,m}^k)) \end{aligned} \quad (19)$$

and $[\pi_{\mu,m}^k, m = 1, \dots, M] = \mu(s^k)$. Hence, the expected utility-to-go $J_{\mu}^k(s^k)$ is also separable and $J_{\mu,m}^k(W_{TCP}^k, N_m^k)$ is also a nondecreasing function of N_m^k . By backward induction, $J_{\mu}^k(s^k), \forall s^k \in \mathcal{S}, k = 1, \dots, K$ are all separable. ■

APPENDIX C

Proof of Theorem 2: From (11), the optimal policy in time slot i with state s^i is the action that maximize the expected utility. Based on Theorem 1, we can see that when the packets in the buffer are independent, the utility-to-go is separable. From (19), the optimization problem becomes the first equation at the bottom of the page. In other words, we have (20), shown at the bottom of the page. Hence, by defining $PM_m^{i*}(s^i) = J_1 - J_0$

in (20), it is clear that with the binary action space, the packet should be transmitted when $PM_m^{i*}(s^i) > 0$ in order to maximize the expected utility (i.e., the problem becomes an optimal stopping problem [23]). ■

APPENDIX D

Proof of Theorem 4: Let $|\mathbf{V}| = 1$, the sufficient condition in (17) is satisfied. Without loss of generality, let $\bar{Q}_1 \geq \bar{Q}_2 \geq \dots \geq \bar{Q}_h \geq \bar{Q}_{h+1} = \mathcal{Q}$. Suppose that the condition is satisfied when $|\mathbf{V}| \leq h$, i.e.,

$$\sum_{n=1}^h (\bar{Q}_n)^2 \sum_{n=1}^h \Delta \bar{Q}_n \geq \sum_{n=1}^h \bar{Q}_n \sum_{n=1}^h \bar{Q}_n \Delta \bar{Q}_n. \quad (21)$$

For $|\mathbf{V}| = h + 1$, since $\mathcal{Q} \leq \bar{Q}_n, \forall V_n \in \mathbf{V}$, if the sufficient conditions are satisfied, we have priority metrics $\Delta \mathcal{Q} = \sum_{\forall m \in \mathbf{M}_{h+1}^k} Q_m N_{m,h+1} \geq \sum_{\forall m \in \mathbf{M}_n^k} Q_m N_{mn} = \Delta \bar{Q}_n, \forall V_n \in \mathbf{V}$. Hence, we have

$$\begin{aligned} \sum_{n=1}^h \Delta \mathcal{Q} \bar{Q}_n (\bar{Q}_n - \mathcal{Q}) &\geq \sum_{n=1}^h \mathcal{Q} \Delta \bar{Q}_n (\bar{Q}_n - \mathcal{Q}) \\ &\Rightarrow \mathcal{Q}^2 \sum_{n=1}^h \Delta \bar{Q}_n + \Delta \mathcal{Q} \sum_{n=1}^h \bar{Q}_n^2 \\ &\geq \mathcal{Q} \sum_{n=1}^h \bar{Q}_n \Delta \bar{Q}_n + \mathcal{Q} \Delta \mathcal{Q} \sum_{n=1}^h \bar{Q}_n. \end{aligned}$$

Adding the above equation and (21), we have

$$\begin{aligned} \left(\sum_{n=1}^h \bar{Q}_n^2 + \mathcal{Q}^2 \right) \left(\sum_{n=1}^h \Delta \bar{Q}_n + \Delta \mathcal{Q} \right) \\ \geq \left(\sum_{n=1}^h \bar{Q}_n + \mathcal{Q} \right) \left(\sum_{n=1}^h \bar{Q}_n \Delta \bar{Q}_n + \mathcal{Q} \Delta \mathcal{Q} \right) \end{aligned}$$

which satisfy the condition in (17). By induction, we prove that the sufficient condition of the lemma is fulfilled for all $|\mathbf{V}| \geq 1$. ■

$$\begin{aligned} &[\pi_1^{i*}(s^i), \dots, \pi_M^{i*}(s^i)] \\ &= \arg \max_{[\pi_1, \dots, \pi_M]} \sum_{m=1}^M \left(\left(Q_m - \frac{\lambda}{W_{TCP}^i} \right) N_m^i \pi_m + \right. \\ &\quad \left. \gamma \sum_{s^{i+1} \in \mathcal{S}} P(W_{TCP}^{i+1}|W_{TCP}^i) J_{\mu,m}^{i+1}(W_{TCP}^{i+1}, N_m^{i+1}(\pi_m)) \right) \end{aligned}$$

$$\begin{aligned} &J_{\mu,m}^i(W_{TCP}^i, N_m^i) \\ &= \begin{cases} J_1 = \left(Q_m - \frac{\lambda}{W_{TCP}^i} \right) N_m^i + \\ \quad \gamma \sum_{s^{i+1} \in \mathcal{S}} P(W_{TCP}^{i+1}|W_{TCP}^i) J_{\mu,m}^{i+1}(W_{TCP}^{i+1}, N_m^{i+1}), & \text{if } \pi_m^{i*} = 1 \\ J_0 = \gamma \sum_{s^{i+1} \in \mathcal{S}} P(W_{TCP}^{i+1}|W_{TCP}^i) J_{\mu,m}^{i+1}(W_{TCP}^{i+1}, N_m^i - N_m^{D,i} + N_m^{A,i}), & \text{if } \pi_m^{i*} = 0 \end{cases} \end{aligned} \quad (20)$$

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