

# A New Systematic Framework for Autonomous Cross-Layer Optimization

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**Abstract**—Cross-layer optimization solutions have been proposed in recent years to improve the performance of wireless users that operate in a time-varying, error-prone network environment. However, these solutions often rely on centralized cross-layer optimization solutions that violate the layered network architecture of the protocol stack by requiring layers to provide access to their internal protocol parameters to other layers. This paper presents a new systematic framework for cross-layer optimization, which allows each layer to make autonomous decisions to maximize the wireless user's utility by optimally determining what information should be exchanged among layers. Hence, this cross-layer framework preserves the current layered network architecture. Since the user interacts with the wireless environment at various layers of the protocol stack, the cross-layer optimization problem is solved in a layered fashion such that each layer adapts its own protocol parameters and exchanges information (messages) with other layers that cooperatively maximize the performance of the wireless user. Based on the proposed layered framework, we also design a message-exchange mechanism that determines the optimal cross-layer transmission strategies, given the user's experienced environment dynamics.

**Index Terms**—Autonomous decision making, cross-layer optimization, environmental dynamics, information exchange, layered dynamic programming (DP) operator.

## I. INTRODUCTION

THE OPEN systems interconnection (OSI) model [1] is a layered abstract organization of various communication and computer network protocols. In layered network architectures, each layer autonomously controls and optimizes a subset of decision variables (i.e., protocol parameters) based on the information (or observations) obtained from other layers to provide services to the layer(s) above. The advantage of layered architectures is that the designer or implementer of the protocol or algorithm at a particular layer can focus on the design of that layer, without being required to consider all the parameters and algorithms of the rest of the stack [3]. However, in current layered network architectures, the information exchange between multiple layers is often implemented in an ad hoc manner. This generally results in suboptimal performance for the users and their applications.

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To optimize the different protocol parameters, the wireless users (transmitter and receiver pairs) need to consider the dynamic wireless network “environment” shaped by the repeated interaction with other users, the time-varying channel conditions, and, for delay-sensitive applications, the time-varying traffic characteristics. Moreover, it should be noted that to maximize its utility, a wireless user needs to jointly optimize the protocol parameters selected at each layer of the OSI stack. The joint optimization of the transmission strategies at the various layers is referred to as *cross-layer optimization* [2], [3]. Recently, various cross-layer optimization methods have been proposed to jointly adapt the transmission strategies at each layer to the rapidly varying network environment. A brief review of this work is presented next.

### A. Related Work

**Application-Specific Solutions:** Numerous solutions have been proposed in recent years to provide efficient adaptation of specific applications (e.g., real-time multimedia transmission) to error-prone networks (e.g., Internet and wireless networks) [25]. A majority of these solutions consider the lower layers as a “black box” and adapt the application (APP) layer strategies based on the information fed back from the lower layers (e.g., information about the network congestion and packet loss rates), as shown in Fig. 1(a). These solutions aim at providing applications the information necessary to adapt their own algorithms and parameters, without exposing the details of the lower layers' protocols and algorithms to the applications. These application-specific solutions, however, often ignore the adaptability of lower layers [e.g., transport layer, network layer, media access control (MAC) layer, and physical (PHY) layer].

**Layer-Centric Solutions:** To jointly consider the lower layers' adaptation, numerous solutions have also been proposed to allow the APP layer to drive the adaptation of network parameters and algorithms by permitting the application to access the internal protocol parameters of the lower layers [2], as shown in Fig. 1(b). Alternative solutions are also developed to allow a certain layer (e.g., the MAC layer) other than the APP layer to drive the cross-layer adaptation by accessing the internal protocol parameters and algorithms of the other layers [4]–[6], as shown in Fig. 1(c). Although these approaches jointly adapt the cross-layer strategies and significantly improve the overall user's performance, they *violate* the layered network architecture, since they require access to the internal variables of other layers. This violation of the layered network architecture has several disadvantages. These disadvantages include creating more dependencies between layers and increasing the

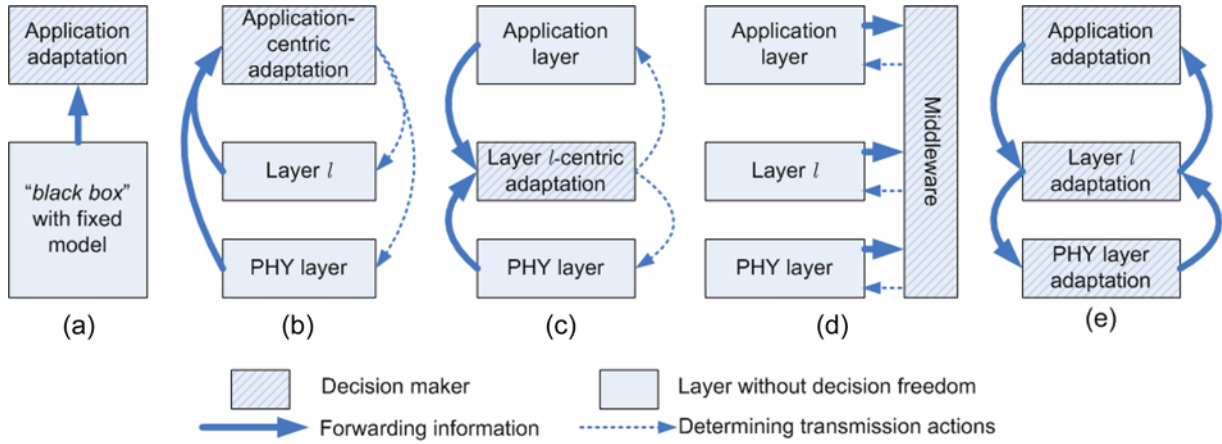


Fig. 1. Conceptual illustration of cross-layer optimization methods. (a) Application adaptation. (b) Application-centric adaptation. (c) Middle layer-centric adaptation. (d) Middleware-based adaptation. (e) Proposed autonomous adaptation with information exchange.

90 difficulty of independent protocol and algorithm design at the  
91 various OSI layers, since one layer needs to be aware of the  
92 parameters of the other layers [3].

93 *Centralized Solutions:* Another type of cross-layer optimi-  
94 zation involves the use of middleware or system-level monitors  
95 (centralized optimizers) to estimate resource availability and  
96 environmental dynamics, coordinate the allocation of resources  
97 across applications and nodes, and adapt the protocols' algo-  
98 rithms and parameters at each layer based on the experienced  
99 dynamics [15], as shown in Fig. 1(d). These solutions typically  
100 coordinate a subset of the system layers and maximize the  
101 user's utility, given all the various resource constraints (e.g.,  
102 power and delay). First, it is clear that the centralized cross-  
103 layer optimization solutions require each layer to forward the  
104 complete information about its protocol-dependent dynamics,  
105 as well as its possible protocol parameters and algorithms, to  
106 the middleware or system-level monitors. Hence, this central-  
107 ized decision also *violates* the current layered network archi-  
108 tecture [3]. Second, the centralized optimization obliges each  
109 layer to take the actions (i.e., select the protocol parameters and  
110 algorithms) dictated by the central optimizer. The layers have  
111 no freedom to adapt their own actions to the environmental  
112 dynamics (e.g., source and channel characteristics) that they  
113 experience. Hence, inherently, each layer loses the authority to  
114 design and select its own suite of protocols and algorithms in-  
115 dependently of the other layers, thereby inhibiting the upgrade  
116 of the protocols and algorithms at each layer.

117 In summary, most existing cross-layer design solutions opti-  
118 mize the protocol parameters in an integrated fashion by jointly  
119 and simultaneously considering the dynamics at each layer and  
120 requiring layers to provide access to their internal protocol  
121 parameters to other layers. These cross-layer interactions create  
122 the dependencies among the layers, which will affect not only  
123 the concerned layer, but also the other layers. Hence, a majority  
124 of these integrated approaches violate the layered network  
125 architecture of the protocol stack, thereby requiring a complete  
126 redesign of current networks and protocols and leading to  
127 a high implementation cost [3]. Another limitation of many  
128 existing cross-layer solutions is that they react to the expe-  
129 rienced network dynamics in a "myopic" way by optimizing  
130 the transmission strategies based on the information about the

current network dynamics and current application requirements 131  
[2], [8], [9]. As shown in our preliminary work [14], to obtain 132  
an optimal utility, applications need to adopt *foresighted* adap- 133  
tation, which considers not only the immediate network status, 134  
but how the network dynamics evolve over time as well. 135

### B. Key Features of the Proposed Framework 136

In this paper, we focus on developing a new systematic 137  
framework for cross-layer optimization based on *foresighted* 138  
decision making such that the selected transmission strategies at 139  
each layer depend not only on the immediate reward, but also 140  
on their impact on the future reward. Moreover, the proposed 141  
framework *preserves* the current layered architecture of the 142  
protocol stack by allowing the layers to make autonomous 143  
decisions based on their locally experienced dynamics and mes- 144  
sage exchanges among the layers, as shown in Fig. 1(e). Thus, 145  
the proposed cross-layer solution is compliant with existing 146  
protocols and standards available at various layers. 147

Similar to works in [15], [17], [19], and [20], we model the 148  
cross-layer optimization problem as a Markov decision process 149  
(MDP) [11] that has as its objective the maximization of the 150  
discounted sum of future utility. This way, the impact of the cur- 151  
rently selected cross-layer transmission strategy on the future 152  
utility (reward) is formulated in a systematic manner. The pro- 153  
posed cross-layer design formulation is presented in Section III. 154

Traditionally, the MDP problem is solved using value itera- 155  
tion or policy iteration algorithms [12]. The key component of 156  
these algorithms is the dynamic programming (DP) operator. In 157  
the current cross-layer optimization literature, the DP operator 158  
is deployed in a centralized way, i.e., the transmission strategies 159  
of all the layers are jointly and simultaneously determined by 160  
a central optimizer or a middleware, as shown in Fig. 1(d). 161  
The disadvantages of this centralized solution have been dis- 162  
cussed in Section I-A. In this paper, we propose a layered 163  
DP operator that complies with the layered architecture and 164  
protocol design of current wireless networks. Using this layered 165  
DP operator, each layer makes its transmission decision [i.e., 166  
selects the transmission strategies, e.g., packet scheduling in the 167  
APP layer, retransmission in the MAC layer, and modulation 168  
selection in the PHY layer] in an autonomous manner by 169

170 considering the dynamics experienced at that layer, as well as  
 171 the information available from other layers. Importantly, this  
 172 layered optimization framework preserves the current layered  
 173 network architecture and does not require each layer to access  
 174 the internal protocol parameters of other layers. This feature  
 175 is desired for the layered network architecture since different  
 176 layers of the protocol stack may be implemented by different  
 177 companies, which may not desire to provide access to their  
 178 parameters and algorithms to other layers that are developed  
 179 by other companies.

180 Specifically, to exchange information across multiple layers,  
 181 we define a message exchange mechanism in which the *content*  
 182 of the message captures the performed transmission strategies  
 183 and experienced dynamics at each layer. However, the *format*  
 184 of the message is independent of the transmission strategies,  
 185 protocols, and dynamics implemented at each layer and can  
 186 be implemented using any agreed-upon signaling protocol [18].  
 187 Hence, the various protocols can be kept the same, upgraded or  
 188 entirely modified; the algorithms at the various layers can also  
 189 be upgraded; and the supported applications can be changed  
 190 without affecting the proposed cross-layer design framework.  
 191 Furthermore, certain layers or algorithms can decide not to  
 192 exchange any messages or not to participate in the cross-layer  
 193 optimization.

194 In summary, this paper makes the following contributions.

- 195 1) We propose a new theoretic cross-layer optimization  
 196 framework that provides a systematic, rather than ad hoc,  
 197 mechanism for dynamically selecting and adapting the  
 198 transmission strategy at each layer and the message ex-  
 199 change across layers. A layered DP operator is proposed  
 200 such that each layer autonomously makes its transmission  
 201 decision by considering its own experienced network  
 202 dynamics and message exchanges from other layers. This  
 203 layered optimization framework does not require a central  
 204 decision maker to consider all the layers' parameters,  
 205 constraints, protocols, algorithms, etc.
- 206 2) A message-exchange mechanism between the layers is  
 207 developed, in which messages capture the experienced  
 208 dynamics and the performed transmission strategies, but  
 209 the format of the message is independent of the transmis-  
 210 sion strategies, deployed protocols, and dynamics experi-  
 211 enced at each layer.

212 Hence, the proposed cross-layer framework keeps the layered  
 213 network architecture unaltered and provides network design-  
 214 ers the freedom of a scalable, flexible, and easily upgradable  
 215 network design.

### 216 C. Paper Organization

217 The rest of this paper is organized as follows. Section II  
 218 discusses the problem settings for the cross-layer optimization.  
 219 Section III briefly reviews the centralized DP operator to solve  
 220 the MDP-based cross-layer optimization problem. Section IV  
 221 presents a layered DP operator framework and discusses the  
 222 advantages of the layered DP operator. Section V gives an  
 223 illustrative example to verify the efficiency of the layered DP  
 224 operator. This paper concludes in Section VI.

## II. CROSS-LAYER PROBLEM FORMULATION

225

We consider an autonomous wireless user transmitting its 226  
 time-varying traffic to another wireless user (e.g., base station) 227  
 over a one-hop wireless network (e.g., wireless local area 228  
 network and cellular network). We study how this wireless user 229  
 can autonomously adapt its transmission strategies<sup>1</sup> at the APP, 230  
 MAC, and PHY layers to maximize its utility. We assume that 231  
 there are  $L$  participating layers<sup>2</sup> in the protocol stack. Each 232  
 layer is indexed  $l \in \{1, \dots, L\}$ , with layer 1 corresponding to 233  
 the lowest participating layer (e.g., PHY layer) and layer  $L$  cor- 234  
 responding to the highest participating layer (e.g., APP layer). 235  
 In this paper, we focus on user-centric cross-layer adaptation, 236  
 where the wireless user performs cross-layer adaptation of the 237  
 $L$  layers to maximize its own utility. 238

Although the cross-layer optimization framework proposed 239  
 in this paper is general, can be applied in different wireless net- 240  
 work settings, and can involve a variety of network protocols, 241  
 we would like to first provide a concrete example of a cross- 242  
 layer optimization problem to help readers become familiar 243  
 with the concept of actions and states before we formally define 244  
 them in Sections II-B and C. 245

### A. Illustrative Cross-Layer Optimization Example

246

Similar to [15], in this example, we consider that the wireless 247  
 user transmitting delay-sensitive data accesses the wireless 248  
 channel. The channel access can be based on time-division 249  
 multiple access (TDMA) or on asynchronous code-division 250  
 multiple access (A-CDMA). In the PHY layer, the wireless user 251  
 experiences the channel noise (e.g., additive Gaussian noise [1]) 252  
 and interference from the other users due to imperfect synchro- 253  
 nization or code design [1]. In cellular networks, interference 254  
 can also be incurred from neighboring cells. The channel qual- 255  
 ity experienced by the wireless user is represented by the signal- 256  
 to-interference-plus-noise ratio (SINR), which is determined by 257  
 the transmission power, channel noise, and interference. Given 258  
 the power allocation, the channel quality is often modeled as a 259  
 finite-state Markov chain (FSMC) [16], [26]. In this example, 260  
 we consider a more general case in which the channel quality is 261  
 modeled as an FSMC with the state transition being controlled 262  
 by the power allocation. Given the SINR, the wireless user 263  
 also adapts the modulation schemes to determine the service 264  
 provided to the upper layers. 265

In the MAC layer, if the channel access is based on TDMA, 266  
 the amount of time allocated to the wireless user during one 267  
 time slot depends on the scheduling algorithm deployed in the 268  
 network, e.g., the predetermined scheduling in the 802.11e 269  
 hybrid coordination function [10] or the repeated resource 270  
 competition discussed in [14]. In the resource competition 271  
 scenario, the wireless user will need to autonomously and 272  
 dynamically compete for transmission time with other users. 273  
 In both resource-management scenarios, we can use an FSMC 274

<sup>1</sup> In this paper, we focus on wireless transmission over one-hop networks, and thus, the transmission strategies at the transport layer and network layer are not considered.

<sup>2</sup> If one layer does not participate in the cross-layer design, it can simply be omitted. Hence, we consider here only the  $L$  participating layers.

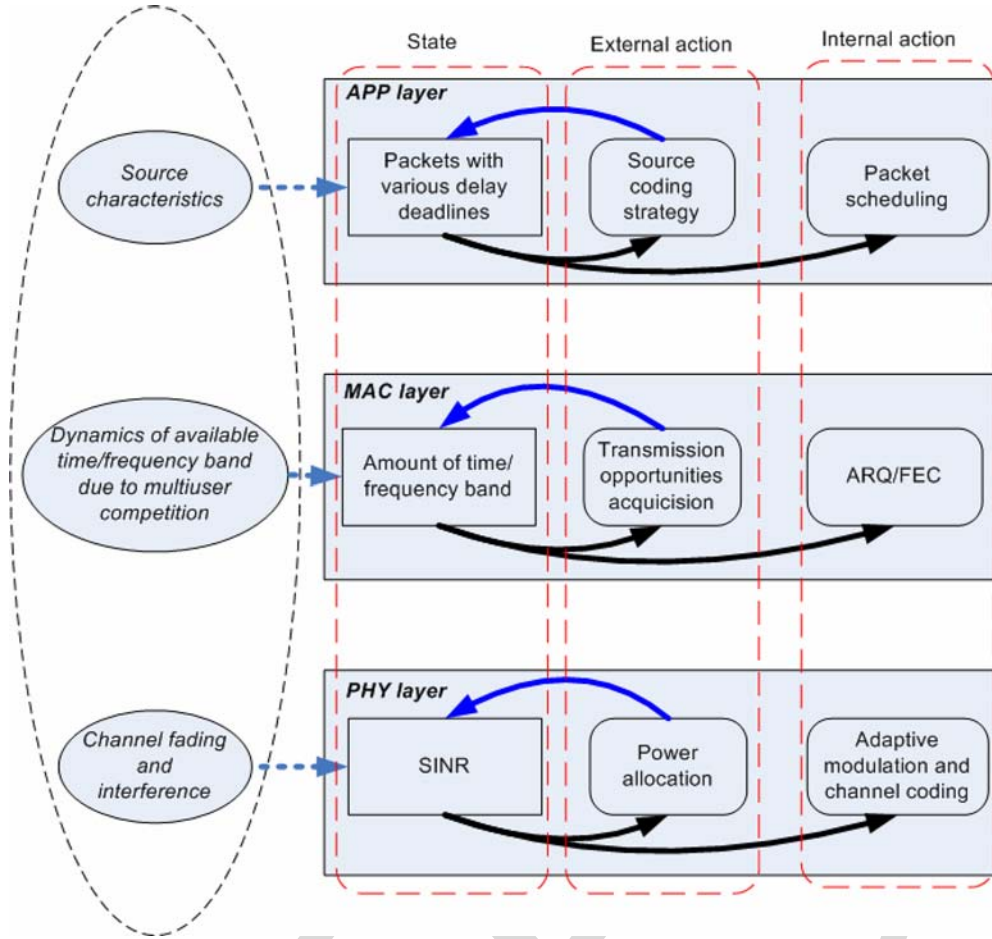


Fig. 2. Internal and external actions and states for the cross-layer optimization in the example.

275 that has as its states the amount of time allocated to the wireless  
 276 user to model the resource-allocation process. However, the  
 277 state transition of the FSMC is determined by the user's  
 278 strategies to compete for the network resources with other  
 279 wireless users (e.g., the bid strategy in the resource auction  
 280 game [14] in the MAC layer). If the resource allocation is  
 281 predetermined, then the process is then controlled by a constant  
 282 action. This model can capture the dynamics experienced by  
 283 a user due to the multiuser interaction. If the channel access  
 284 is based on A-CDMA, then the wireless users can access the  
 285 channel all the time. The state transition is a special case of  
 286 FSMC with the state being constant. In addition to the resource  
 287 allocation, the MAC can also perform error control algorithms  
 288 such as Automatic Repeat-reQuest (ARQ) or forward error  
 289 correction (FEC) to improve the service provided to the upper  
 290 layers.

291 In the APP layer, we assume that the wireless user generates  
 292 delay-sensitive traffic. The delay sensitivity is represented by  
 293 the delay deadlines after which the packets will expire, and  
 294 thus, they will not contribute to the wireless user's application  
 295 quality. As in [15], we can model the number of packets with  
 296 the various delay deadlines available for transmission as an  
 297 FSMC. Since the transmission strategies at the lower layers  
 298 determines the amount of packets to be transmitted and the  
 299 source coding algorithms determines the amount of packets to  
 300 arrive for transmission, the state transition is then controlled by

the transmission strategies at the lower layers and the source- 301  
 coding algorithms. 302

The objective of the wireless user is to jointly adapt the 303  
 transmission strategies across all the three layers such that the 304  
 user's utility is maximized. 305

### B. States 306

In wireless communication, different states can be defined 307  
 at each layer to capture the currently experienced dynamics 308  
 [12], [15]. In this paper, the state of the layers is defined such 309  
 that future transmission strategies can be determined indepen- 310  
 dently of the past history of the transmission strategies and 311  
 environment, given the current state, i.e., the state is Markovian. 312  
 To adhere to the layered architecture of current networks, we 313  
 define a state  $s_l \in \mathcal{S}_l$  for each layer  $l$ . Then, the state of the 314  
 entire wireless user is denoted by  $s = (s_1, \dots, s_L) \in \mathcal{S}$ , with 315  
 $\mathcal{S} = \mathcal{S}_1 \times \dots \times \mathcal{S}_L$ . The states of the cross-layer optimization 316  
 example are illustrated in Fig. 2. 317

### C. Actions 318

In a layered architecture, a wireless user takes different trans- 319  
 mission actions in each state of each layer. The transmission 320  
 actions can be classified into two types at each layer  $l$ : An 321  
*external action* is performed to determine what the next state 322

323 should be (i.e., state transition) such that the future reward will  
324 be improved, and an *internal action* is performed to determine  
325 the service provided to the upper layers for the packet(s)  
326 transmission in current time slot.

327 The external actions at each layer  $l$  are denoted by  $a_l \in A_l$ ,  
328 where  $A_l$  is the set of the possible external actions available  
329 at layer  $l$ . The external actions of the wireless user at all the  
330 layers are denoted by  $a = (a_1, \dots, a_L) \in A$ , where  $A = A_1 \times$   
331  $\dots \times A_L$ . The internal actions are denoted by  $b_l \in B_l$ , where  
332  $B_l$  is the set of the possible internal actions available at layer  $l$ .  
333 The internal actions are performed by the wireless user to  
334 efficiently *utilize* the allocated wireless network resource and its  
335 own resource budget (e.g., power constraint) by providing the  
336 quality of service (QoS) required by the supported applications.  
337 The internal actions of the wireless user across all the layers are  
338 denoted by  $b = (b_1, \dots, b_L) \in B$ , where  $B = B_1 \times \dots \times B_L$ .  
339 The action at layer  $l$  is the aggregation of external and internal  
340 actions, which is denoted by  $\xi_l = (a_l b_l) \in \mathcal{X}_l$ , where  $\mathcal{X}_l =$   
341  $A_l \times B_l$ . The joint action of the wireless user is denoted by  $\xi =$   
342  $(\xi_1, \dots, \xi_L) \in \mathcal{X} = \mathcal{X}_1 \times \dots \times \mathcal{X}_L$ . The external and internal  
343 actions in the cross-layer optimization example are illustrated  
344 in Fig. 2.

345 Distinguishing between the internal and external transmis-  
346 sion actions has the following advantages, which will become  
347 clearer in Section IV.

- 348 1) The current utility computation based on the internal  
349 actions can be computed independently of the state  
350 transition that takes place due to the external actions  
351 deployed at each layer. This separation enables us to  
352 design a cross-layer optimization framework that complies  
353 with the current layered architecture of the protocol  
354 stack.
- 355 2) The separation between the internal actions and external  
356 actions enables us to design an interlayer message  
357 exchange mechanism that is independent of the specific  
358 format of the protocols and algorithms deployed at each  
359 layer.

#### 360 D. Transition Probability

361 In this section, we examine the structure of the state transition  
362 model and the underlying models for environmental dynamics.  
363 In general, because states are Markovian, the state transition  
364 of the wireless user only depends on the current state  $s$ ,  
365 the current performed external actions, and the environmental  
366 dynamics. The corresponding transition probability is denoted  
367 by  $p(s'|s, \xi)$ . This global state transition can be compactly  
368 represented using a dynamic decision network [22]. Formally,  
369 the transition model is decomposed as

$$p(s'|s, \xi) = \prod_{l=1}^{L-1} p(s'_l | \text{parent}(s'_l), \text{action}(s'_l)) \quad (1)$$

370 where  $\text{parent}(s'_l)$  represents the set of states on which the  
371 transition of  $s'_l$  depends, and  $\text{action}(s'_l)$  represents the set of  
372 actions performed at the current time that affect the transi-  
373 tion of  $s'_l$ .

In the cross-layer optimization example, the state transition  
at each layer  $l < L$  is only controlled by the external actions  
at that layer and is independent of the other layers' states and  
actions. At layer  $L$ , the state transition is determined by the  
external actions at that layer and internal actions of all the  
layers. Motivated by this example, we can further simplify  
the transition probability for the cross-layer optimization as

$$p(s'|s, \xi) = \prod_{l=1}^{L-1} p(s'_l | s_l, a_l) p(s'_L | s, a_L, \mathbf{b}). \quad (2)$$

Comparing (2) with (1), we note that  $\text{parent}(s'_l) = \{s_l\}$  and  
 $\text{action}\{s'_l\} = \{a_l\}$  for  $l \in \{1, \dots, L-1\}$ , and  $\text{parent}(s'_L) =$   
 $\{s\}$  and  $\text{action}\{s'_L\} = \{a_L, \mathbf{b}\}$ . In other words, the state tran-  
sition at the lower layer ( $l \in \{1, \dots, L-1\}$ ) is driven by the  
external action  $a_l$  at that layer and depends only on its own  
current state  $s_l$ . At layer  $L$ , the state transition is determined  
using both the external action  $a_L$  as well as the internal actions  
 $\mathbf{b}$  at all the layers. We also allow the state transition at layer  $L$  to  
depend on the current states  $s$  of all the layers. We should note  
that although the state transition in the lower layers ( $l < L$ ) is  
independent of other layers' state, the external action selection  
at that layer will depend on the message (e.g., the future reward  
generated by the upper layer) exchanged with the other layers,  
which will be specified in Sections IV-C and D. Fig. 3 illustrates  
how the state transition is determined.

This decomposition is determined such that the cross-layer  
optimization is complying with the layered network architec-  
ture and enables the development of a layered framework for  
cross-layer optimization, which will be presented in Section IV.

#### E. Utility Function

The application quality obtained in layer  $L$  is based on the  
states and internal actions at each layer and is denoted by  
 $g(s, \mathbf{b})$ . At the same time, performing the internal actions at  
various layers will incur the internal cost  $d(s, \mathbf{b})$ , and it will  
be set to zero if no cost is incurred. The external cost  $c_l(s_l, a_l)$   
at layer  $l$  represents the cost of performing the external action,  
e.g., the amount of power allocated to determine the channel  
conditions or the tax (tokens, money) spent for consuming wire-  
less resources [13], [14]. The utility gain and the corresponding  
costs are depicted in Fig. 3. In this paper, we have defined the  
reward as

$$R(s, \xi) = g(s, \mathbf{b}) - \lambda^b d(s, \mathbf{b}) - \sum_{l=1}^L \lambda_l^a c_l(s_l, a_l) \quad (3)$$

where  $\lambda^b$  and  $\lambda_l^a$  are positive parameters that trade off be-  
tween the application quality and cost incurred by performing  
certain actions. These parameters can be determined based on  
the resource budgets available for the wireless user [17] or  
by the network coordinator to efficiently utilize the network  
resources [24]. In this paper, we assume that these parameters  
are known to the wireless users, and we focus on the internal  
and external action selection for utility maximization. The  
reward in (3) can be further decomposed into the following  
two parts: 1) the internal reward, which depends on the internal

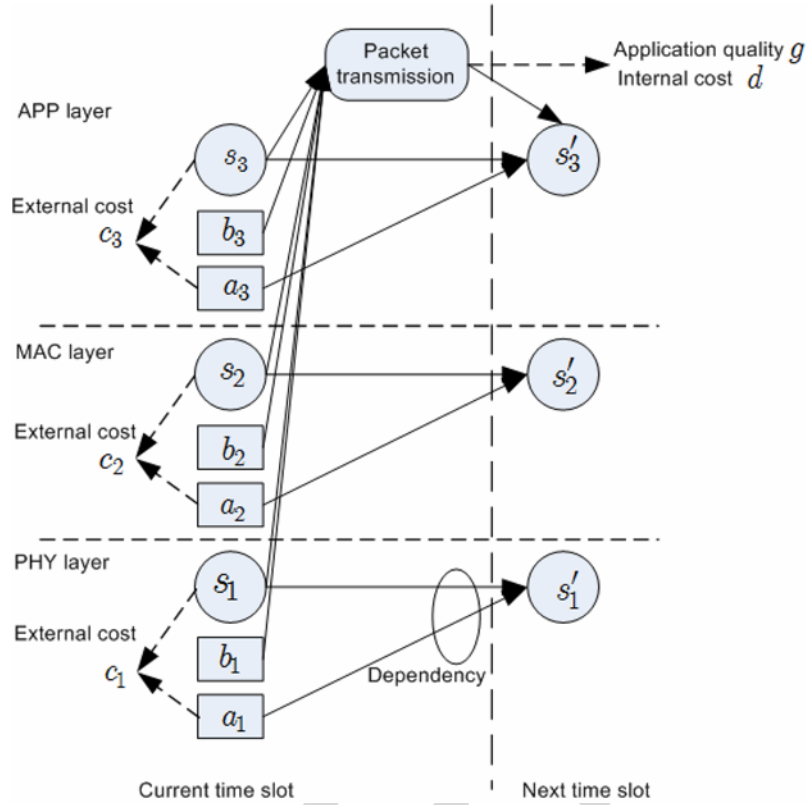


Fig. 3. Layered transition model and components of decomposed utility function.

422 actions; and 2) the external reward, which depends on the  
423 external actions. The internal reward is

$$R_{\text{in}}(\mathbf{s}, \mathbf{b}) = g(\mathbf{s}, \mathbf{b}) - \lambda^b d(\mathbf{s}, \mathbf{b}) \quad (4)$$

424 and the external reward is

$$R_{\text{ex}}(\mathbf{s}, \mathbf{a}) = - \sum_{l=1}^L \lambda_l^a c_l(s_l, a_l). \quad (5)$$

425 Hence, the reward is  $R = R_{\text{in}} + R_{\text{ex}}$ .

#### 426 F. MDP Formulation for Foresighted 427 Cross-Layer Optimization

428 As described in Section II-D, the state transition at each  
429 layer is controlled by the external actions. For simplicity, we  
430 assume that the state transition in each layer is synchronized  
431 and operates at the same time scale such that the transition  
432 can be discretized into stages during which the wireless user  
433 has constant state and performs static actions. The length of  
434 the stage is denoted by  $\Delta T$  and can be determined based on  
435 how fast the environment changes. We use a superscript  $k$  to  
436 denote stage  $k$ . Hence, the state of the wireless user at stage  
437  $k \in \mathbb{N}$  is denoted by  $\mathbf{s}^k$ , with each element  $s_l^k$  being the state  
438 of layer  $l$ ; similarly, the joint action performed by the wireless  
439 user at stage  $k$  is  $\boldsymbol{\xi}^k$ , with each element  $\xi_l^k = (a_l^k, b_l^k)$ . The state  
440 transition probability is given by (2), and the stage reward is  
441 given by (3).

442 Unlike the conventional cross-layer adaptation that focuses  
443 on maximizing the myopic (i.e., immediate) utility, in the pro-

posed cross-layer framework, the goal is to find the optimal in- 444  
ternal and external actions at each stage such that a cumulative 445  
function of the rewards is maximized. We refer to this decision 446  
process as the *foresighted* cross-layer decision. By maximizing 447  
the cumulative reward, the wireless user is able to take into 448  
account the impact of the current actions on the future reward. 449  
Specifically, we assume that the wireless user will maximize the 450  
discounted accumulative reward, which is defined as 451

$$\sum_{k=0}^{\infty} (\gamma)^k R(\mathbf{s}^k, \boldsymbol{\xi}^k | \mathbf{s}^0) \quad (6)$$

where  $\gamma$  is a discounted rate with  $0 \leq \gamma < 1$ , and  $\mathbf{s}^0$  is the 452  
initial state. Unlike the formulation in [17] and [21], where 453  
the time-average reward is considered, we use a discounted 454  
accumulated reward with a higher weight on the current reward. 455  
The reasons for this are given as follows: 1) For delay-sensitive 456  
applications, the data need to be sent out as soon as possible 457  
to avoid missing delay deadlines; and 2) since a wireless user 458  
may encounter unexpected environmental dynamics in the 459  
future, it may care more about its immediate reward. Hence, 460  
this needs to be considered when determining the values of 461  
 $\gamma$  for a specific cross-layer problem. 462

The foresighted cross-layer optimization can be formulated 463  
using an MDP, which is defined as follows. 464

*Definition 1 (MDP):* An MDP is defined [11] as a tuple  $M =$  465  
 $\langle \mathcal{S}, \mathcal{X}, p, R, \gamma \rangle$ , where  $\mathcal{S}$  is a joint state space, i.e.,  $\mathcal{X}$  is a joint 466  
action space for each state,  $p$  is a transition probability function 467  
 $\mathcal{S} \times \mathcal{X} \times \mathcal{S} \mapsto [0, 1]$ ,  $R$  is a reward function  $\mathcal{S} \times \mathcal{X} \mapsto \mathfrak{R}$ , and 468  
 $\gamma$  is the discounted factor. 469

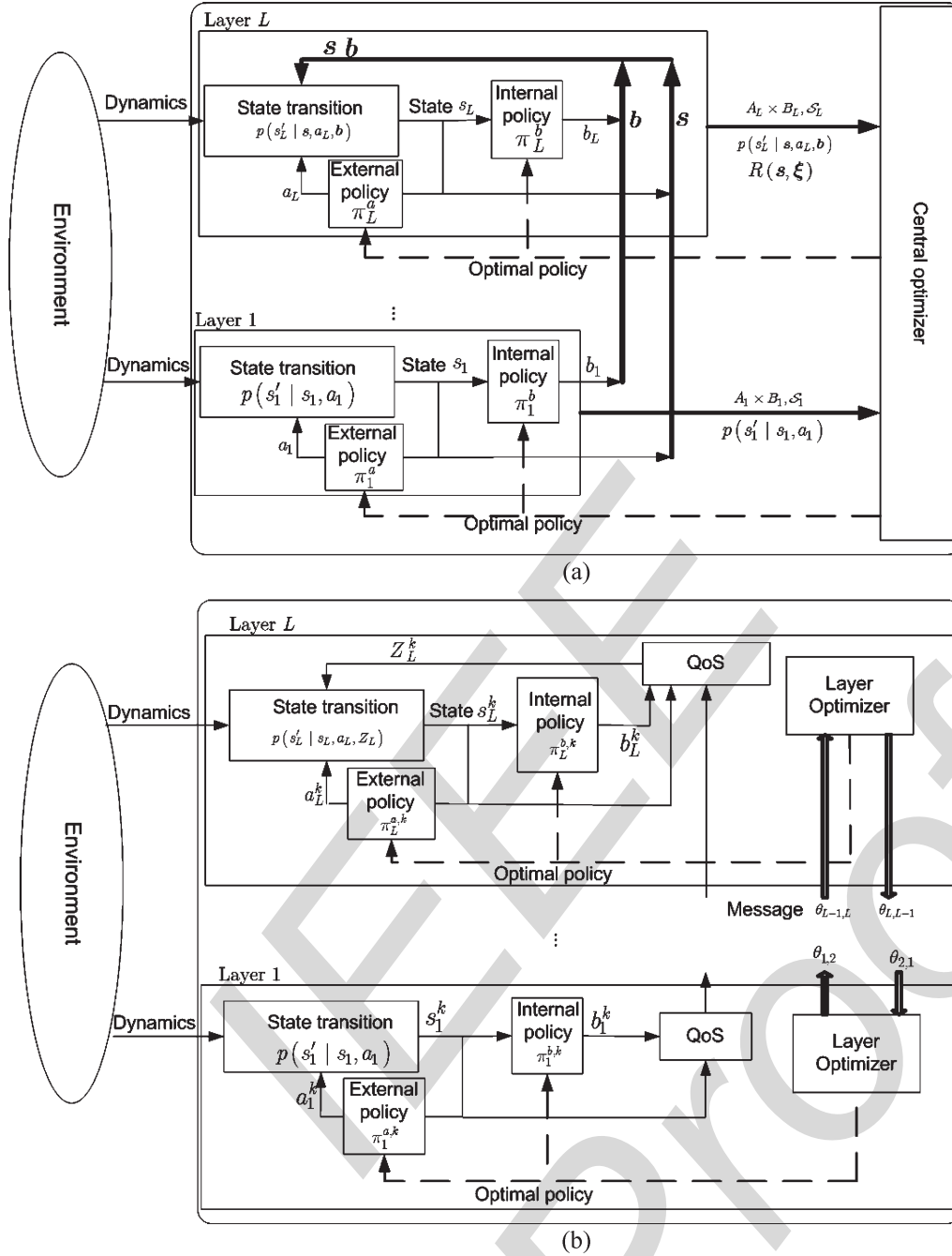


Fig. 4. Comparison of traditional cross-layer optimization framework and proposed cross-layer optimization framework. (a) Centralized cross-layer optimization framework. (b) Layered cross-layer optimization framework.

470 In our context, the joint state space is  $\mathcal{S} = \mathcal{S}_1 \times \dots \times \mathcal{S}_L$ ,  
 471 the joint action space is given by  $\mathcal{X} = \mathcal{X}_1 \times \dots \times \mathcal{X}_L$ , the  
 472 transition probability is given by (2), and the reward function  
 473 is given by (3).

### 474 III. CENTRALIZED CROSS-LAYER SOLUTION 475 AND ITS DISADVANTAGES

#### 476 A. Centralized Cross-Layer Optimization

477 Similar to [7], [15], and [17], the foresighted cross-layer op-  
 478 timization can be solved in a centralized way without noticing  
 479 the structure of the cross-layer optimization. To solve the MDP

problem, the central optimizer needs to know the following [see 480  
 Fig. 4(a)]: 481

- 1) the state space at each layer; 482
- 2) the action space at each layer; 483
- 3) probability distribution describing the state transition 484  
 (i.e., environmental dynamics); 485
- 4) state reward function of the states and performed actions. 486

Several centralized algorithms (e.g., the policy iteration, 487  
 value iteration, and linear programming [12]) have been pro- 488  
 posed to find the optimal policy that maximizes the discounted 489  
 sum of future rewards. However, these algorithms neglect the 490  
 layered structure of the cross-layer optimization. 491

492 In both the value-iteration and policy-iteration algorithms,  
 493 the key step that needs to be performed at each iteration is  
 494 solving the following optimization:

$$\max_{\xi \in \mathcal{X}} \left\{ R(s, \xi) + \gamma \sum_{s' \in \mathcal{S}} p(s'|s, \xi) V(s') \right\} \quad (7)$$

495 where  $V(s')$  is a state-value function defined as the discounted  
 496 reward that can be received when starting from state  $s'$ .

497 This optimization is called the DP operator [12]. In  
 498 Section IV, we will decompose this key step into the layered  
 499 DP operator such that the MDP problem can be solved in the  
 500 manner that complies with the network architecture.

#### 501 B. Limitations Associated With Centralized 502 Cross-Layer Optimization

503 In the centralized optimization described in Section III-A, the  
 504 actions at all the layers are simultaneously selected in the DP  
 505 operator. However, this centralized optimization exhibits the  
 506 following problems when implemented in the layered network  
 507 architectures.

508 First, from Fig. 4(a), it is clear that the centralized cross-  
 509 layer optimization solution requires each layer to forward the  
 510 complete information about its protocol-dependent dynamics,  
 511 as well as its internal and external action space and state  
 512 space to the central optimizer. This centralized decision violates  
 513 the current layered network architecture [3]. Specifically, a  
 514 completely new interface between the central optimizer and all  
 515 the layers is created. The central optimizer is allowed to access  
 516 the internal variables at each layer, and hence, it is required to  
 517 know the details about the protocols and algorithms deployed  
 518 at each layer.

519 Second, the centralized optimization obliges each layer to  
 520 take actions specified by the central optimizer. The layers have  
 521 no freedom to adapt their own actions to the environmental  
 522 dynamics that they experience. Hence, inherently, each layer  
 523 loses the power to design its own protocol independently of  
 524 other layers, which inhibits the upgrade of the various layers'  
 525 protocols and algorithms.

#### 526 IV. LAYERED CROSS-LAYER OPTIMIZATION

527 To overcome the problems associated with the centralized  
 528 cross-layer optimization that violates the layered network archi-  
 529 tecture, in this paper, we design a layered DP operator, which  
 530 takes advantage of the structure of the cross-layer optimization  
 531 discussed in Section II and allows each layer to autonomously  
 532 optimize its own policy, based on the information exchanged  
 533 with the other layers. This way, the layered architecture is  
 534 preserved.

535 We will first discuss in Section IV-A how one layer can  
 536 abstract the QoS that it provides to its upper layer and how it can  
 537 compute the internal reward defined in (4). In Section IV-B, we  
 538 discuss how the DP operator in (7) can be decomposed to com-  
 539 ply with the layered architecture of the protocol stack and what  
 540 messages are required to be exchanged among layers for this  
 541 decomposition. In Section IV-C, we discuss how the internal  
 542 and external actions are selected from the layered DP operator.

#### A. Quality of Service and Internal Reward Computation 543

In the layered network architecture, each layer selects its own  
 544 internal actions, which, combined with the service provided by  
 545 the lower layers, determine the QoS supported to the upper  
 546 layer. In examples 1 and 2, the QoS levels computed in the  
 547 PHY layer and provided to the MAC layer at the current time  
 548 slot include the data throughput (in packets per second), the  
 549 packet error rate, and the cost for transmitting one packet. The  
 550 services are determined by the internal actions (e.g., modulation  
 551 adaptation) and the state [i.e., signal-to-noise ratio (SNR) or  
 552 SINR]. Based on the services provided by the PHY layer, the  
 553 MAC layer can then adapt the ARQ scheme (e.g., the internal  
 554 action) to compute the throughput, the packet error rate, and the  
 555 cost of transmitting one packet (including the cost in the PHY  
 556 layer), which are provided to the APP layer. 557

In this paper, we consider that each layer  $l$  provides to the  
 558 upper layer the QoS, which includes the following: 1) the  
 559 packet loss probability  $\varepsilon_l$ , which presents the probability that  
 560 one packet at layer  $l$  is lost due to the imperfect trans-  
 561 mission; 2) the transmission time per packet<sup>3</sup>  $\tau_l$  at layer  $l$ ;  
 562 and 3) the transmission cost per packet  $v_l$  at layer  $l$ . The  
 563 QoS at layer  $l$  is denoted by  $Z_l = (\varepsilon_l, \tau_l, v_l)$ . The QoS  
 564  $Z_l$  is determined by the internal actions  $b_l$  and the QoS  
 565  $Z_{l-1}$  from the lower layer  $l-1$ , i.e.,  $Z_l = (\varepsilon_l, \tau_l, v_l) =$   
 566  $(f_l^\varepsilon(s_l, b_l, Z_{l-1}), f_l^\tau(s_l, b_l, Z_{l-1}), f_l^v(s_l, b_l, Z_{l-1}))$ , where  $f_l^\varepsilon$ ,  
 567  $f_l^\tau$ , and  $f_l^v$  are the functions that map the current state  $s_l$   
 568 and internal action  $b_l$  at layer  $l$  and the QoS  $Z_{l-1}$  at layer  
 569  $l-1$  into the packet loss rate  $\varepsilon_l$ , transmission time  $\tau_l$ , and  
 570 transmission cost  $v_l$ , respectively. For notation simplicity, here,  
 571 we denote the functions compactly as  $Z_l = \vec{f}_l(s_l, b_l, Z_{l-1})$ . The  
 572 specific forms of these functions depend on the applications and  
 573 network protocols. In Section V, we will give the specific forms  
 574 of these functions for the example illustrated in Section II-A.  
 575 Given the QoS at layer  $L$ , the application quality  $g(s, b)$   
 576 only depends on the packet loss rate and transmission time  
 577 and is then computed as  $g(s, b) = g(s_L, \varepsilon_L, \tau_L)$ . The inter-  
 578 nal cost  $d(s, b)$  is computed as  $d(Z_L) = v_L$ . The internal  
 579 reward function is computed as  $R_{\text{in}}(s, b) = R_{\text{in}}(s_L, Z_L) =$   
 580  $g(s_L, \varepsilon_L, \tau_L) - \lambda^b v_L$ . 581

To compute the internal reward function  $R_{\text{in}}(s_L, Z_L)$ , layer  
 582  $L$  has to know all the QoS levels jointly determined by the states  
 583 and internal actions at all the layers. Given the current state  $s$   
 584 of the wireless user, the set of the possible QoS levels at layer  $l$   
 585 is denoted by  $Z_l(s)$  and can be computed by enumerating all the  
 586 combinations of internal actions available at each layer, i.e., 587

$$Z_l(s) = \left\{ Z_l \mid Z_l = \vec{f}_l(s_l, b_l, Z_{l-1}), \dots, Z_1 = \vec{f}_1(s_1, b_1, \emptyset) \right. \\ \left. \forall b_1 \in B_1, \dots, b_l \in B_l \right\}. \quad (8)$$

Then, the set of QoS levels  $Z_l(s)$  at layer  $l$  captures the nec-  
 588 essary information from the lower layers to compute the inter-  
 589 nal reward. In the layered network architecture, using the QoS  
 590 set, layer  $l+1$  does not need to know the actions and states of  
 591 the lower layers. However, the size of the set  $Z_l(s)$  is often 592

<sup>3</sup>The transmission time per packet is the duration (time) for which the packet is being transmitted.



593 very large and, hence, leads to a high computational burden  
594 at the higher layers. In the following, we present a method to  
595 reduce the number of QoS levels to be provided to the upper  
596 layer without the performance loss.

597 We first define the relationship between two QoS levels at  
598 layer  $l$  using the following two terms: 1) “dominated” and  
599 2) “Pareto equivalent.”

600 **Definition 2 (Dominated QoS):** A QoS  $Z_L = (\varepsilon_L, \tau_L, v_L)$  is  
601 dominated with respect to another QoS  $Z'_L = (\varepsilon'_L, \tau'_L, v'_L)$  if  
602  $\varepsilon'_L \leq \varepsilon_L$ ,  $\tau'_L \leq \tau_L$ ,  $v'_L \leq v_L$ , and the equalities do not hold at  
603 the same time (i.e.,  $Z'_L - Z_L \leq 0^4$  but  $Z'_L \neq Z_L$ ). We denote this

604 relationship as  $Z'_L \stackrel{d}{\leq} Z_L$ .

605 **Definition 3 (Pareto-Equivalent QoS):** A QoS  $Z_L = (\varepsilon_L,$   
606  $\tau_L, v_L)$  is Pareto equivalent to another QoS  $Z'_L = (\varepsilon'_L, \tau'_L, v'_L)$ ,  
607 which is denoted by  $Z'_L \stackrel{p}{\sim} Z_L$ , if neither of the QoS levels is

608 dominated by the other, i.e.,  $Z'_L \stackrel{d}{\leq} Z_L$  or  $Z_L \stackrel{d}{\leq} Z'_L$ .

609 Based on the relationship definition, we notice that for two  
610 QoS levels  $Z'_L = (\varepsilon'_L, \tau'_L, v'_L)$  and  $Z_L = (\varepsilon_L, \tau_L, v_L)$ , if  $Z'_L \stackrel{d}{\leq}$   
611  $Z_L$ , then  $g(s_L, \varepsilon'_L, \tau'_L) \geq g(s_L, \varepsilon_L, \tau_L)$ , since the lower packet  
612 loss probability and smaller transmission time per packet lead to  
613 more packets being transmitted and, hence, a higher application  
614 quality. Therefore, we have  $R_{\text{in}}(s_L, Z'_L) \geq R_{\text{in}}(s_L, Z_L)$ .

615 Furthermore, if layer  $l-1$  provides two QoS levels  $Z_{l-1}$   
616 and  $Z'_{l-1}$ , with  $Z'_{l-1} \stackrel{d}{\leq} Z_{l-1}$ , then  $Z'_l = \vec{f}_l(s_l, b_l, Z'_{l-1}) \leq Z_l =$   
617  $\vec{f}_l(s_l, b_l, Z_{l-1}) \forall s_l \in \mathcal{S}_l, b_l \in B_l$ . That is, the functions  $f_l^\varepsilon$ ,  $f_l^\tau$ ,  
618 and  $f_l^v$  are nondecreasing functions of  $Z_{l-1}$ , given the current  
619 state  $s_l \in \mathcal{S}_l$  and internal action  $b_l \in B_l$ . This can be explained  
620 as follows: When layer  $l-1$  provides lower packet loss rate  
621  $\varepsilon'_{l-1}$ , lower transmission time per packet  $\tau'_{l-1}$ , and lower trans-  
622 mission cost per packet  $v'_{l-1}$ , the internal action  $b_l$  at the current  
623 state  $s_l$  at layer  $l$  will result in lower packet loss rate  $\varepsilon'_l$ , lower  
624 transmission time per packet  $\tau'_l$ , and lower transmission cost  
625 per packet  $v'_l$ . For example, at the MAC layer, given a lower  
626 packet loss rate, a lower transmission time per packet, and a  
627 lower transmission cost per packet from the PHY layer, the  
628 same ARQ scheme (e.g., the same number of retransmission)  
629 will give a lower packet loss rate, a lower transmission time per  
630 packet, and a lower transmission cost per packet as well.

631 Hence, in our cross-layer design framework, the states and  
632 actions preserve the “domination” relationship of the QoS  
633 levels. That is, the states and actions in each layer have the  
634 following property.

635 **Property 1 (Preservation of QoS):** If  $Z'_{l-1} \stackrel{d}{\leq} Z_{l-1}$ , then  
636  $Z'_l = \vec{f}_l(s_l, b_l, Z'_{l-1}) \leq Z_l = \vec{f}_l(s_l, b_l, Z_{l-1}) \forall s_l \in \mathcal{S}_l, b_l \in B_l$ .  
637 The preservation of QoS means that the dominated QoS  
638  $Z_l$  provided by layer  $l$  cannot result in a dominant QoS by  
639 performing any internal action at the upper layer. Hence, the  
640 dominated QoS  $Z_l$  should not be reported to the upper layer.  
641 Hence, the preservation of the domination relationship signif-  
642 icantly reduces the amount of information exchanged by the  
643 lower layers to the upper layers. To describe the QoS levels that  
644 must be provided to the upper layer, we first define the optimal  
645 QoS frontier.

**Definition 4 (Optimal QoS Frontier):** The optimal frontier  
646 of the possible QoS set  $Z_l(s)$  at layer  $l$  is the largest subset  
647  $\tilde{Z}_l(s) \subseteq Z_l(s)$  with each element satisfying the following  
648 condition: For any  $Z_l \in Z_l(s)$ , there is no existing  $\tilde{Z}_l \in Z_l(s)$  649

such that  $\tilde{Z}_l \stackrel{d}{\leq} Z_l$ . 650

Hence, each layer  $l$  is only required to provide the QoS set 651  
 $\tilde{Z}_l(s)$  that represents the optimal frontier instead of all the 652  
possible QoS levels (i.e.,  $Z_l$ ). The algorithm to construct the 653  
QoS frontier at layer  $l$  is presented in Algorithm 1. 654

Algorithm 1. Method for constructing the optimal QoS 655  
frontier  $\tilde{Z}_l$  656

**Input:**  $Z_{l-1}$ ,  $s_l$ , and  $B_l$ . 657

**Initialize:**  $Z_l = \emptyset$ , flag = 0. 658

**Loop 1:** For each  $b_l \in B_l$  659

**Loop 2:** For each  $Z_{l-1} \in Z_{l-1}$  660

flag = 0; 661

Compute  $Z_l = \vec{f}_l(s_l, b_l, Z_{l-1})$ . 662

**Loop 3:** For each  $Z'_l \in Z_l$  663

If  $Z'_l \stackrel{d}{\leq} Z_l$  664

flag = 1; break; 665

endif 666

endfor //loop 3 667

if flag == 0 668

$Z_l = Z_l \cup \{Z_l\}$ . 669

endif 670

endfor //loop 2 671

endfor // loop 1 672

## B. Layered DP Operator 673

The key step of the cross-layer optimization is the DP 674  
operator. In the centralized formulation, the DP operator can 675  
only be performed in a centralized manner. In this section, we 676  
show how to decompose the DP operator into a layered DP with 677  
information exchange among the layers. 678

Considering the structure of the cross-layer optimization 679  
explored in Section II, we can rewrite the DP operator in (7) 680  
as follows: 681

$$\left. \begin{aligned} & \max_{\mathbf{a} \in \mathbf{A}, \mathbf{b} \in \mathbf{B}} \left\{ \underbrace{g(\mathbf{s}, \mathbf{b}) - \lambda^b d(\mathbf{s}, \mathbf{b}) - \sum_{l=1}^L \lambda_l^a c_l(s_l, a_l)}_{R(\mathbf{s}, \boldsymbol{\xi})} \right. \\ & \left. + \gamma \underbrace{\sum_{s'_1 \in \mathcal{S}_1, \dots, s'_L \in \mathcal{S}_L} p(s'_1 | s_1, a_1) \cdots p(s'_L | \mathbf{s}, \mathbf{b}, a_L) V(s'_1, \dots, s'_L)}_{\sum_{s' \in \mathcal{S}} p(s' | \mathbf{s}, \boldsymbol{\xi}) V(s')} \right\}. \end{aligned} \right\} \quad (9)$$

<sup>4</sup> $X \geq 0$  means that every component of  $X$  is greater than or equal to 0.

TABLE I  
DP OPERATOR AT EACH LAYER

Layer	DP operator at each layer
$L$	$V_{L-1}(s'_1, \dots, s'_{L-1}) = \max_{\substack{a_L \in A_L, \\ Z_L \in \mathcal{Z}_L}} \left[ R_m(s_L, Z_L) - \lambda_L^a c_L(s_L, a_L) + \gamma \sum_{s'_L \in \mathcal{S}_L} p(s'_L   s_L, Z_L, a_L) V(s'_1, \dots, s'_L) \right]$
$l \in \{2, \dots, L-1\}$	$V_{l-1}(s'_1, \dots, s'_{l-1}) = \max_{a_l \in A_l} \left[ -\lambda_l^a c_l(s_l, a_l) + \sum_{s'_l \in \mathcal{S}_l} p(s'_l   s_l, a_l) V_l(s'_1, \dots, s'_l) \right]$
1	$V \langle \mathbf{s} \rangle = \max_{a_1 \in A_1} \left[ -\lambda_1^a c_1(s_1, a_1) + \sum_{s'_1 \in \mathcal{S}_1} p(s'_1   s_1, a_1) V_1(s'_1) \right]$

TABLE II  
MESSAGE EXCHANGES BETWEEN LAYERS FOR LAYERED DP OPERATOR

Layer	Upward Message $\theta_{l,l+1}$		Downward Message $\theta_{l,l-1}$	
$L$	$\emptyset$	None	$\{V_{L-1}(s'_1, \dots, s'_{L-1})\}$	Expected future reward at layer $L-1$
$l \in \{2, \dots, L-1\}$	$\mathcal{Z}_l$	QoS level set provided to layer $l+1$	$\{V_{l-1}(s'_1, \dots, s'_{l-1})\}$	Expected future reward at layer $l-1$
1	$\mathcal{Z}_1$	QoS level set provided to layer 2	$\emptyset$	None

682 In the layered DP operator, we allow each layer to select its  
683 own internal and external actions to perform the optimization,  
684 as shown in (9). From the Appendix, the DP operator can be  
685 performed at each layer as shown in Table I, and the message  
686 exchanges between layers are shown Table II.

687 In this layered DP operator, the optimal external action  
688  $a_l^l(s'_1, \dots, s'_{l-1})$  is selected for each state  $(s'_1, \dots, s'_{l-1})$  at the  
689 lower layers, and the optimal QoS level  $Z_L^l(s'_1, \dots, s'_{L-1})$  de-  
690 pends on the state  $(s'_1, \dots, s'_{L-1})$ . Then, we have the following  
691 theorem.

692 *Theorem 1:* The state-value functions obtained in the layered  
693 DP operator satisfy the follow inequalities:

$$\begin{aligned}
 & V_{L-1}(s'_1, \dots, s'_{L-1}) \\
 &= \max_{\substack{a_L \in A_L, \\ Z_L \in \mathcal{Z}_L}} \left[ R_{\text{in}}(s_L, Z_L) - \lambda_L^a c_L(s_L, a_L) \right. \\
 &\quad \left. + \gamma \sum_{s'_L \in \mathcal{S}_L} p(s'_L | s_L, Z_L, a_L) V(s'_1, \dots, s'_L) \right] \\
 &\geq R_{\text{in}}(s_L, Z_L^*) - \lambda_L^a c_L(s_L, a_L^*) \\
 &\quad + \gamma \sum_{s'_L \in \mathcal{S}_L} p(s'_L | s_L, Z_L^*, a_L^*) V(s'_1, \dots, s'_L) \\
 &\quad \forall (s'_1, \dots, s'_{L-1}) \quad (10)
 \end{aligned}$$

$$\begin{aligned}
 & V_{l-1}(s'_1, \dots, s'_{l-1}) \\
 &= \max_{a_l \in A_l} \left[ -\lambda_l^a c_l(s_l, a_l) + \sum_{s'_l \in \mathcal{S}_l} p(s'_l | s_l, a_l) V_l(s'_1, \dots, s'_l) \right] \\
 &\geq -\lambda_l^a c_l(s_l, a_l^*) + \sum_{s'_l \in \mathcal{S}_l} p(s'_l | s_l, a_l^*) V_l(s'_1, \dots, s'_l) \\
 &\quad \forall (s'_1, \dots, s'_{l-1}), \quad \forall l = 1, \dots, L-1 \quad (11)
 \end{aligned}$$

where the optimal external actions  $a_l^* \forall l$  and optimal QoS level  
 $Z_L^*$  are obtained in the centralized DP operator.

*Proof:* The inequalities in (10) and (11) result from the  
fact that  $a_l^* \forall l$  and  $Z_L^*$  represent the feasible solution to the lay-  
ered DP operator, and hence, the state-value function obtained  
by the layered DP operator (which performs the maximization)  
is greater than or equal to the state-value function of any  
feasible solution. The detailed proof is omitted here due to  
space limitations. ■

Theorem 1 shows that the layered DP operator obtains higher  
state-value functions by performing the mixed actions at each  
layer, as explained below.

Similar to the centralized DP operator, at layer  $l$ , given the  
next state  $(s'_1, \dots, s'_{l-1})$  and current state  $s$ , the optimal external  
action  $a_l^l(s'_1, \dots, s'_{l-1})$  obtained in the layered DP operator is a  
pure action. However, the next state  $(s'_1, \dots, s'_{l-1})$  is unknown  
at the current stage and has the probability distribution  $p(s'_1 |$   
 $s_1, a_1^l), p(s'_2 | s_2, a_2^l(s')), \dots, p(s'_{l-1} | s_{l-1}, a_{l-1}^l(s'_1, \dots, s'_{l-1}))$

TABLE III  
MESSAGE EXCHANGE FOR INTERNAL AND EXTERNAL ACTION SELECTION

Layer	Upward Message $\theta_{l,l+1}$		Downward Message $\theta_{l,l-1}$	
$L$	$\emptyset$	None	$Z_{L-1}^\dagger$	The optimal QoS at layer $L-1$
$l \in \{2, \dots, L-1\}$	$\arg \max_{s'_1} p(s'_1   s_1, a_1^\dagger)$ $\vdots$ $\arg \max_{s'_l} p(s'_l   s_l, a_l^\dagger)$	The optimal next states at layers $1, \dots, l$	$Z_{l-1}^\dagger$	The optimal QoS at layer $l-1$
$1$	$\arg \max_{s'_1} p(s'_1   s_1, a_1^\dagger)$	The optimal next state	$\emptyset$	None

determined by the external actions performed at layers  $1, \dots, l-1$  and the environmental dynamics. Hence, the optimal external action  $a_l^m(s)$  at layer  $l$  (computed without knowing the next states at layers  $1, \dots, l-1$ ) is a mixed action, whose elements  $a_l^\ell(s'_1, \dots, s'_{l-1})$  have the same probability distribution as that of  $(s'_1, \dots, s'_{l-1})$ , i.e.,  $p(s'_1 | s_1, a_1^\dagger), p(s'_2 | s_2, a_2^\dagger), \dots, p(s'_{l-1} | s_{l-1}, a_{l-1}^\dagger(s'_1, \dots, s'_{l-1}))$ . Then, we can represent the mixed external action at layer  $l$  as

$$a_l^m(s) = \bigcup_{s'_1 \in \mathcal{S}_1, \dots, s'_{l-1} \in \mathcal{S}_{l-1}} \left\{ p(s'_1 | s_1, a_1^\dagger), p(s'_2 | s_2, a_2^\dagger(s'_1)), \dots, p(s'_{l-1} | s_{l-1}, a_{l-1}^\dagger(s'_1, \dots, s'_{l-1})) \circ a_l^\ell(s'_1, \dots, s'_{l-1}) \right\} \quad (12)$$

where the operator “ $\circ$ ” indicates that action  $a_l^\ell(s'_1, \dots, s'_{l-1})$  is performed with the probability  $p(s'_1 | s_1, a_1^\dagger), p(s'_2 | s_2, a_2^\dagger(s'_1)), \dots, p(s'_{l-1} | s_{l-1}, a_{l-1}^\dagger(s'_1, \dots, s'_{l-1}))$ . We use the union operator “ $\cup$ ” to compactly represent the mixed action. Similarly, the optimal QoS level at layer  $L$  is given by

$$Z_L^m(s) = \bigcup_{s'_1 \in \mathcal{S}_1, \dots, s'_{L-1} \in \mathcal{S}_{L-1}} \left\{ p(s'_1 | s_1, a_1^\dagger), p(s'_2 | s_2, a_2^\dagger(s'_1)), \dots, p(s'_{L-1} | s_{L-1}, a_{L-1}^\dagger(s'_1, \dots, s'_{L-1})) \circ Z_L^\ell(s'_1, \dots, s'_{L-1}) \right\}. \quad (13)$$

In summary, compared with the centralized DP operator in which the pure action is chosen for each current state  $s$ , the optimal pure action  $a_l^\ell(s'_1, \dots, s'_{l-1})$  in the layered DP operator is chosen for each current state  $s$  and next state  $(s'_1, \dots, s'_{l-1})$ . In other words, the layered DP operator takes into account the states' information at the next stage [i.e.,  $(s'_1, \dots, s'_{l-1})$ ] and performs the mixed actions based on the distribution of the states  $(s'_1, \dots, s'_{l-1})$ . Hence, the optimal mixed actions can improve the state-value function.

### C. Internal and External Actions Selection

In this section, we will illustrate how the internal and external actions are selected without knowing the states at the next stage in the layered DP operator. From (12) and (13), we notice that

the layered DP operator can only provide the mixed actions. The mixed action selection at each layer requires the transition probabilities at the lower layers. However, in our proposed layered network architecture, we do not allow the exchange of transition probabilities (i.e., the dynamics model at that layer), since this leads to significantly increased information exchange and requires each layer to access the internal parameters of other layers, thereby violating the OSI layer design. Instead, we restrict the optimal external action and optimal QoS-level selection as follows:

$$\begin{aligned} a_1^\dagger &= a_1^\ell \\ a_2^\dagger &= a_2^\ell \left( \arg \max_{s'_1} p(s'_1 | s_1, a_1^\dagger) \right) \\ &\vdots \\ a_L^\dagger &= a_L^\ell \left( \arg \max_{s'_1} p(s'_1 | s_1, a_1^\dagger), \dots, \right. \\ &\quad \left. \arg \max_{s'_{L-1}} p(s'_{L-1} | s_{L-1}, a_{L-1}^\dagger) \right) \\ Z_L^\dagger &= Z_L^\ell \left( \arg \max_{s'_1} p(s'_1 | s_1, a_1^\dagger), \dots, \right. \\ &\quad \left. \arg \max_{s'_{L-1}} p(s'_{L-1} | s_{L-1}, a_{L-1}^\dagger) \right). \end{aligned} \quad (14)$$

From (14), we note that the action and QoS-level selection does not require the information of transition probability but rather the states that maximize the transition probability. However, we should note that this selection is an approximation to the optimal mixed action and QoS level. To select external action and QoS level, the lower layer  $l-1$  needs to provide the information  $(\arg \max_{s'_1} p(s'_1 | s_1, a_1), \dots, \arg \max_{s'_{l-1}} p(s'_{l-1} | s_{l-1}, a_{l-1}))$  to layer  $l$ . Given the approximated QoS level  $Z_L^\dagger$ , we obtain the internal action  $b_L^\dagger$  and the QoS level  $Z_{L-1}^\dagger$  at layer  $L-1$ , which generate the QoS level  $Z_L^\dagger$ . Similarly, given the QoS level  $Z_l^\dagger$ , layer  $l$  can find the internal action  $b_l^\dagger$  and the QoS level  $Z_{l-1}^\dagger$  for layer  $l-1$ . Hence, to select the internal action, layer  $l$  needs to provide the information  $Z_{l-1}^\dagger$  to layer  $l-1$ .

### D. Advantages of the Layered DP Operator

In this section, we highlight the advantages of the proposed layered DP operator compared with the centralized DP operator

764 illustrated in Section III-A.

765 As discussed in Section III, the central optimizer is required  
766 to completely know the dynamics model (i.e., states, transition  
767 probability) and possible internal and external actions of all the  
768 layers that are protocol dependent. Hence, the mechanism of  
769 information exchange between the central optimizer and the  
770 layers is also protocol dependent. In the proposed algorithm,  
771 however, the centralized DP operator shown in (7) is decom-  
772 posed into multiple layered DP operators, each of which is  
773 accordingly solved by one layer. From the layered DP operators  
774 shown in Table I and the message exchange between layers  
775 shown in Tables II and III, we note that our proposed layered  
776 DP operator has the following advantages.

777 First, to perform the layered DP operator, given the infor-  
778 mation exchanged between layers, each layer is only required  
779 to know its own internal and external actions and transition  
780 probabilities (corresponding to the dynamics models), but it is  
781 not required to know the actions and transition probabilities of  
782 other layers.

783 Second, the format (i.e., QoS optimal frontier for upward  
784 messages and the state-value functions for downward message)  
785 of the messages exchanged between layers is independent of  
786 the protocols deployed in each layer, while the content (i.e.,  
787 QoS optimal frontier depends on the performed internal actions  
788 and state-value function depends on the external actions) of the  
789 messages characterizes the dynamics and performed actions at  
790 each layer.

791 Third, the internal and external actions are autonomously  
792 selected by each layer. Each layer has its own freedom to  
793 determine its own transmission strategies, which is desirable  
794 for the case that the protocols at various layers are designed  
795 by different companies. This way, upgrading the protocol at  
796 one layer does not affect other layers' protocol designs. Hence,  
797 our proposed cross-layer optimization solution preserves the  
798 current layered network architecture.

## 799 V. SIMULATION RESULTS FOR THE 800 ILLUSTRATIVE EXAMPLE

801 In this section, we use the example presented in Section II-A  
802 to illustrate the proposed cross-layer design framework. We  
803 first discuss the states, actions, and dynamics model used at  
804 each layer. Then, we provide simulation results to illustrate  
805 the merits of our proposed layered DP operator for cross-layer  
806 optimization.

### 807 A. APP Layer Models

808 In the APP layer, we assume that the wireless user deploys  
809 a delay-sensitive application (e.g., streaming "Mobile" video  
810 sequence with a 30-Hz frame rate at common intermediate  
811 format resolution). The data of the APP layer are packetized  
812 with an average packet length  $\eta$  in bits. Each packet is associ-  
813 ated with a hard delay deadline, i.e., it will expire after  $J\Delta T$   
814 seconds ( $J$  stages) after they are ready for transmission. Then,  
815 we can define the state of the APP layer at stage  $k$  as  $s_3^k =$   
816  $[s_{3,1}^k, \dots, s_{3,J}^k]^T$ , where  $s_{3,j}^k$  ( $1 \leq j \leq J$ ) is the number of  
817 packets waiting for transmission that have a remaining lifetime  
818 of  $j$  stages.

In the APP layer, the external action  $a_3^k$  (i.e., the source  
coding algorithms) determines the amount of packets arriving  
into the buffer at the beginning of stage  $k$ . For simplicity, we  
assume that  $a_3^k$  is equal to the average number of arriving  
packets. We denote by  $Y_3^k$  the random number of arriving  
packets. Then,  $E[Y_3^k] = a_3^k$ . The probability mass function of  
the random variable  $Y_3^k$  is assumed to be independent at each  
stage and is denoted by  $\{P(Y_3^k = y|a_3^k), y \in \mathbb{N}\}$ .

Given the QoS  $Z_3^k$ , the APP layer transmits the packets with  
lifetime 1. If there are no packets with lifetime 1 remaining for  
transmission, the packets with lifetime 2 will be transmitted,  
and so on. The number of packets that can be transmitted is  
computed as

$$n_3^k(Z_3^k) = \left\lfloor \frac{\Delta T}{\tau_3^k} (1 - \varepsilon_3^k) \right\rfloor. \quad (15)$$

The state at stage  $k+1$  is updated as

$$\begin{bmatrix} s_{3,1}^{k+1} \\ \vdots \\ s_{3,j}^{k+1} \\ \vdots \\ s_{3,J}^{k+1} \end{bmatrix} = \begin{bmatrix} s_{3,2}^k - \max(n_3^k(Z_3^k) - s_{3,1}^k, 0) \\ \vdots \\ s_{3,j+1}^k - \max\left(n_3^k(Z_3^k) - \sum_{m=1}^j s_{3,m}^k, 0\right) \\ \vdots \\ Y_3^k(a_3^k) \end{bmatrix}. \quad (16)$$

The state transition probability is computed as

$$p(s_3^{k+1}|s_3^k, a_3^k, Z_3^k) = \begin{cases} P(Y_3^k = y|a_3^k), & \text{if } s_3^{k+1} \text{ satisfies the relationship} \\ & \text{in (19) and } Y_3^k = y \\ 0, & \text{o.w.} \end{cases} \quad (17)$$

The application quality for the delay-sensitive application is  
defined here as

$$g(s_3^k, Z_3^k) = n_3^k(Z_3^k) - \lambda_g \max\{s_{3,1}^k - n_3^k(Z_3^k), 0\} \quad (18)$$

where  $\lambda_g$  is the parameter to tradeoff the received packets and  
lost packets. In this simulation, the internal action at layer 3 is  
empty, and hence,  $Z_3^k = Z_2^k$ . In this simulation, we reported the  
video quality in terms of peak SNR (PSNR) to indicate the real  
received video quality in Section V-E.

### 807 B. MAC Layer Model

For the TDMA-based channel access, the MAC layer re-  
quests spectrum access by performing the external actions  $a_2^k$ ,  
which can be the resource requests values (e.g., taxation).  
The MAC layer state  $s_2^k \in [0, 1]$  is the fraction of one time  
slot allocated in the current stage and quantized as a discrete  
value. By taking external action  $a_2^k$ , the transition probability is  
 $p(s_2^{k+1}|s_2^k, a_2^k)$ , and the external cost introduced is  $c_2(s_2^k, a_2^k) =$   
 $a_2^k$ . For the A-CDMA-based channel access, the MAC layer  
does not need to request spectrum access since the whole  
spectrum band is available. Hence, the state at the MAC layer  
is  $s_2^k = 1$ , and the external action  $a_2^k = \emptyset$ . The corresponding

TABLE IV  
PARAMETERS USED FOR THE SIMULATION AT THE VARIOUS LAYERS

Layer	Parameter	
PHY layer	Channel model parameters	$f_d = 50\text{Hz}, T_p = 0.8\text{ms}, s_1 \in [0.4, 0.8, \dots, 4]\text{dB}$
	Modulation level	$m = 1, \dots, 4$ (BPSK, QPSK, 8PSK, 16PSK)
	Power allocation	$A_1 = \{0.5, 1, 1.5, 2\}$
	Packet loss probability <sup>1</sup>	$\varepsilon_1 = 1 - (1 - \text{BER})^\eta$ $\text{BER}(s_1, m) = \text{erfc}\left(\kappa \Gamma_{s_1} \sin\left(\frac{\pi}{2^m}\right)\right), \kappa = 283.5$
	Transmission time per packet	$T_p / m$
MAC layer	MAC state	$s_2 \in \{0.2, 0.4, \dots, 1\}$
	Maximum retransmission limit	$N_{\max} = 5$
	Trade-off parameter $\lambda_2^g$	$\lambda_2^g = 0.1$
	Competition bids (external action)	$A_2 = \{0, 1\}$
	APP state	$s_3 \in \{(0, 0), \dots, (4, 4)\}$
APP layer	Maximum life time	$J = 2$
	External action	$A_3 = \{1, 2, 3\}$
	Trade-off parameter $\lambda_g$	$\lambda_g = 0.1$

853 external cost is 0. The state transition probability is given by  
854  $p(s_2^{k+1} = 1 | s_2^k = 1, a_2^k = \emptyset) = 1$ .

855 The wireless user can perform ARQ to enhance the QoS  
856 provided to the APP layer. Hence, the internal action can be  
857  $b_2^k \in \{0, \dots, N_{\max}\}$ , where  $N_{\max}$  is the maximum retry limit,  
858 and  $b_2^k$  is the actual retry limit. Given the QoS provided from  
859 the PHY layer, e.g.,  $Z_1^k = (\varepsilon_1^k, \tau_1^k, v_1^k)$ , if the internal action  $b_2^k$   
860 is performed, then the QoS obtained in the MAC layer becomes

$$Z_2^k = (\varepsilon_2^k, \tau_2^k, v_2^k) = \left( (\varepsilon_1^k)^{b_2^k+1}, \frac{(1 - (\varepsilon_1^k)^{b_2^k}) \tau_1^k}{(1 - \varepsilon_1^k) s_2^k}, \frac{(1 - (\varepsilon_1^k)^{b_2^k}) v_1^k}{(1 - \varepsilon_1^k)} \right). \quad (19)$$

861 It is easy to show that if  $Z_1^k \stackrel{d.}{\leq} \tilde{Z}_1^k$ , then  $Z_2^k \stackrel{d.}{\leq} \tilde{Z}_2^k$  for any  
862 internal action  $b_2^k$ , which means that the preservation of QoS  
863 property defined in Section III is satisfied.

#### 864 C. PHY Layer Model

865 Similar to the model used in [15] and [16], we assume  
866 that the received SINR experienced by a wireless user can  
867 be modeled as a discrete time FSMC. The state  $s_1^k$  in the  
868 PHY layer is the SINR. At each state, the wireless user is  
869 able to adapt its modulation and channel coding scheme (i.e.,  
870 internal action)  $b_1 \in B_1$  to determine the QoS level to support  
871 upper layer, where  $B_1$  is the set of possible modulation and  
872 channel coding schemes. The wireless user also has to adapt  
873 the power allocation (i.e., external action)  $a_1 \in A_1$  to determine  
874 the received SINR (i.e., the state at next time slot), where  $A_1$   
875 is the set of possible power allocations. The external cost is  
876  $c_1(s_1^k, a_1^k) = a_1^k$ . As shown in [6], the PHY layer state can be  
877 determined by partitioning the possible received SINR into  $r +$   
878 1 disjoint regions  $\mathbb{R}_0, \dots, \mathbb{R}_r$  by boundary points  $\Gamma_0, \dots, \Gamma_{r+1}$ ,  
879 where  $\mathbb{R}_i = [\Gamma_i, \Gamma_{i+1}]$  and  $\Gamma_0 < \Gamma_1 < \dots < \Gamma_{r+1}$ . The PHY

layer is said to be in the state  $s_1^k = \tilde{\Gamma}_i$ , where  $\tilde{\Gamma}_i$  is the 880  
representative channel gain if the real channel gain is in the 881  
region  $\mathbb{R}_{i-1}$ . Similar to [16], the channel gain is assumed to 882  
be a Rayleigh-fading channel, which is denoted by  $\Upsilon$  and is 883  
exponentially distributed with the following probability density 884  
function: 885

$$p_\Upsilon(\mu) = \frac{1}{\bar{\mu}(a_1)} \exp\left(-\frac{\mu}{\bar{\mu}(a_1)}\right), \quad \mu \geq 0 \quad (20)$$

where  $\bar{\mu}(a_1)$  is the average SINR, which is determined by the 886  
allocated transmission power  $a_1$ . The state transition at the PHY 887  
layer is computed as 888

$$p(s_1^{k+1} | s_1^k, a_1^k) = \begin{cases} \mathcal{N}(\tilde{\Gamma}_{i+1}) \frac{T_p}{\omega_i}, & s_1^k = \tilde{\Gamma}_i, s_1^{k+1} = \tilde{\Gamma}_{i+1} \\ \mathcal{N}(\tilde{\Gamma}_i) \frac{T_p}{\omega_i}, & s_1^k = \tilde{\Gamma}_i, s_1^{k+1} = \tilde{\Gamma}_{i-1} \\ 1 - \mathcal{N}(\tilde{\Gamma}_{i+1}) \frac{T_p}{\omega_i} - \mathcal{N}(\tilde{\Gamma}_i) \frac{T_p}{\omega_i}, & s_1^k = \tilde{\Gamma}_i, s_1^{k+1} = \tilde{\Gamma}_i \\ 0, & \text{o.w.} \end{cases} \quad (21)$$

where  $\mathcal{N}(\mu) = (2\pi\mu/\bar{\mu}(a_1))^{1/2} f_d \exp(-\mu/\bar{\mu}(a_1))$ ,  $\omega_i = 889$   
 $\exp(-\Gamma_i/\bar{\mu}(a_1)) - \exp(-\Gamma_{i+1}/\bar{\mu}(a_1))$ ,  $T_p$  is the transmission 890  
time for one packet, and  $f_d$  is the maximum Doppler 891  
frequency. 892

#### 893 D. Stage Reward Function

In this section, we present the explicit form of the internal 894  
reward function. In this example, the internal cost  $d(s, b)$  is 895  
0, and the internal reward function is given by  $R_{\text{in}}(s_3^k, Z_3^k) = 896$   
 $n_3^k(Z_3^k) - \lambda_g \max\{s_{3,1}^k - n_3^k(Z_3^k), 0\}$ . It is easy to prove that 897  
the internal reward function  $R_{\text{in}}(s_3^k, Z_3^k)$  is a nonincreasing 898  
function of  $Z_3^k$ , i.e.,  $R_{\text{in}}(s_3^k, Z_3^k) \geq R_{\text{in}}(s_3^k, \tilde{Z}_3^k)$  if  $Z_3^k \stackrel{d.}{\leq} \tilde{Z}_3^k$ . 899  
This property enables each layer only to report the QoS frontier 900  
to its upper layer, as discussed in Section IV-A. 901

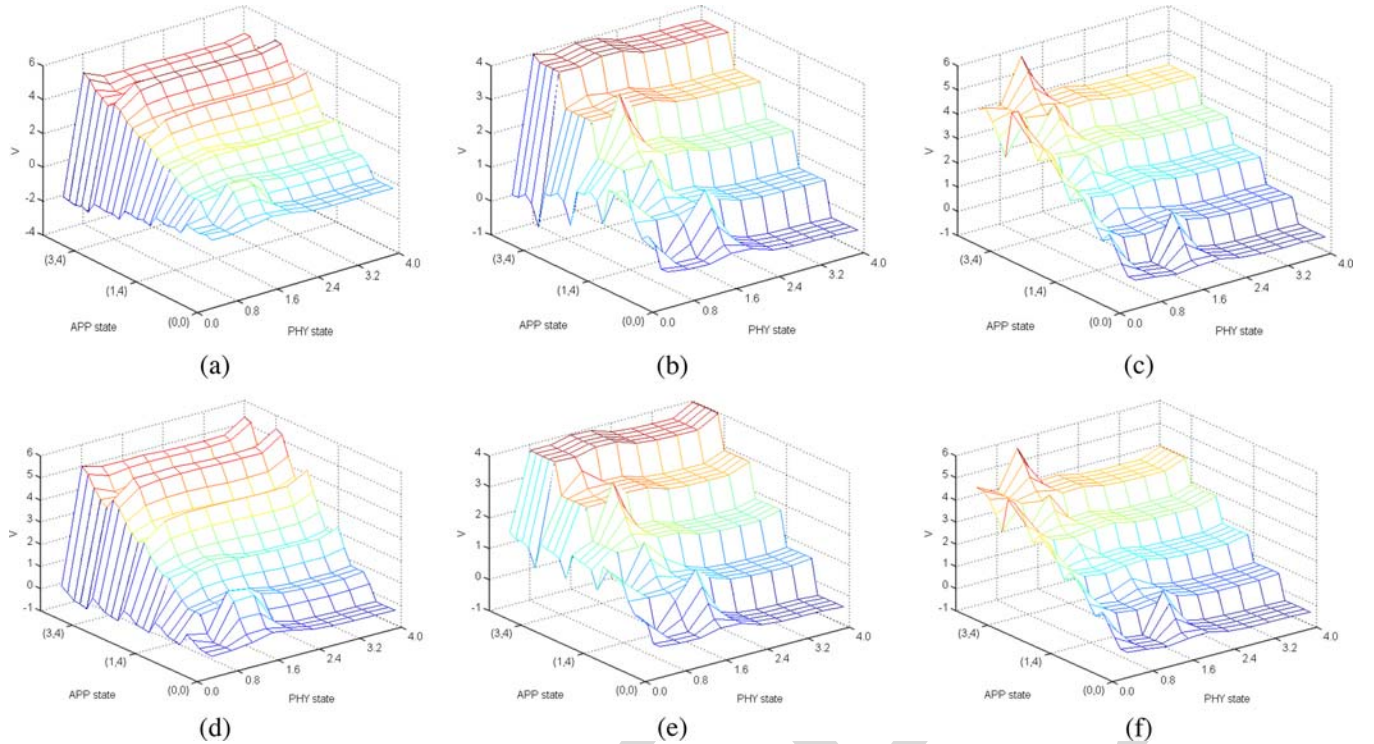


Fig. 5. State-value functions that resulted from the centralized value iteration and proposed layered value iteration. (a)–(c) State-value functions of the centralized DP operator when  $s_2 = 0.1, 0.6,$  and  $1,$  respectively. (d)–(f) State-value functions of the layered DP operator when  $s_2 = 0.1, 0.6,$  and  $1,$  respectively.

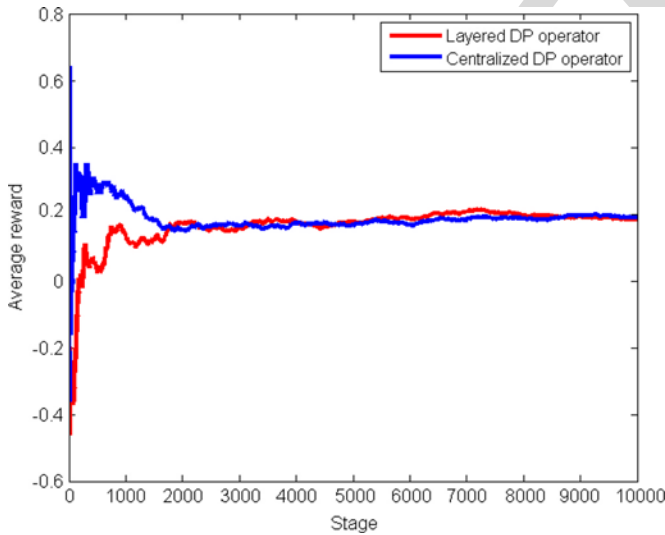


Fig. 6. Average reward obtained using the policies from a centralized DP operator and a layered DP operator.

### 902 E. Simulation Results Verifying the Optimality 903 of the Layered DP Operator

904 We compare the optimal state-value functions obtained using  
905 the centralized DP operator and layered DP operator in the  
906 simulation presented in this section. Through this comparison,  
907 we will verify that the proposed layered DP operator also op-  
908 timally solves the cross-layer optimization problem defined in  
909 Section II. The parameters for the APP, MAC, and PHY layers  
910 are shown in Table IV. The state-value functions  $V^*(s)$  re-  
911 sulting from the centralized DP operator and proposed layered

DP operator are shown in Fig. 5, where we observe that the 912  
state-value functions computed based on both algorithms are 913  
close, which means that our proposed layered DP operator 914  
achieves the performance close to the centralized one, i.e., 915  
near-optimally finding the cross-layer transmission strategies. 916  
To prove that, we also implement the policy obtained by both 917  
algorithms on line. The average rewards are depicted in Fig. 6, 918  
which demonstrates that the performance of both algorithms is 919  
the same when running for a long time. The transient perfor- 920  
mance of the layered DP operator in the beginning is worse 921  
than the central one, which is because we start from the state 922  
in which the centralized DP operator has good performance. 923  
The average PSNRs of the video sequence for both layered 924  
DP operator and centralized DP operator are 32.5 and 32.8 dB, 925  
respectively. 926

### 927 F. Myopic Versus Foresighted Optimization

In this simulation, we use the same parameters as in 928  
Section V-E. We compare the performance of the myopic cross- 929  
layer optimization (i.e.,  $\gamma = 0$ ) versus our proposed foresighted 930  
cross-layer optimization. We first run the value iteration to 931  
solve the cross-layer optimization off-line and apply the optimal 932  
policy on-line. Fig. 7 shows the average reward per stage for 933  
both the myopic policy and foresighted policy. The average 934  
reward obtained by the foresighted policy is 0.1850, while the 935  
average reward by the myopic policy is only  $-0.1050$ . Note 936  
that this reward value is computed based on the utility function 937  
given in Section V-D, and thus, other types of utility functions 938  
may have different values. The simulation results demonstrate 939

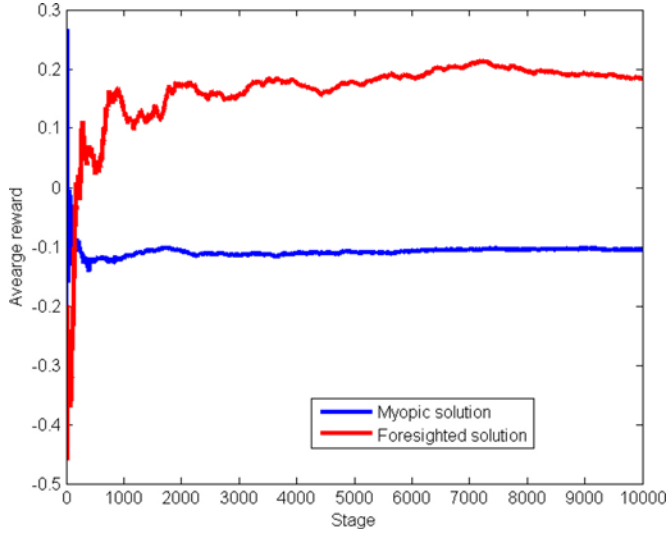


Fig. 7. Average reward per state for myopic cross-layer optimization and foresighted cross-layer optimization.

940 that the foresighted policy can achieve much better performance  
941 than the myopic policy.

942

## VI. CONCLUSION

943 In this paper, we have formulated the dynamic cross-layer  
944 optimization problem as an MDP in which each layer interacts  
945 independently with the environment and experiences different  
946 dynamics. We proposed a layered DP operator to solve the  
947 cross-layer MDP problem. The layered DP operator allows each  
948 layer to perform its own optimization to find the optimal actions  
949 in an autonomous manner, given the information exchanges  
950 with other layers. Each layer is not required to know the  
951 protocols and algorithms implemented at other layers, thereby  
952 complying with the current layered network architecture and  
953 allowing network designers to build scalable, flexible, and  
954 upgradable protocols and algorithms at each layer of the OSI  
955 stack. An important topic for future work is the extension of  
956 this layered cross-layer framework by explicitly considering  
957 the constraints at each layer. Other important topics include  
958 implementing this framework for specific cross-layer problems,  
959 such as power-optimized transmission of media streams, real-  
960 time transmission over different types of channels, and wireless  
961 streaming for different video applications exhibiting various  
962 delay constraints.

## APPENDIX

963

In the layered DP operator, the layers cooperatively perform 964  
the optimization shown in (9). Given the optimal frontier of 965  
QoS levels at layer  $L$ , the DP operator is rewritten as 966

$$\max_{a_1 \in A_1, \dots, a_L \in A_L, Z_L \in \mathcal{Z}_L} \left\{ R_{\text{in}}(s_L, Z_L) - \sum_{l=1}^L \lambda_l^a c_l(s_l, a_l) + \gamma \sum_{s'_1 \in \mathcal{S}_1, \dots, s'_L \in \mathcal{S}_L} p(s'_1 | s_1, a_1), \dots, p(s'_L | s_L, Z_L, a_L) V(s'_1, \dots, s'_L) \right\}. \quad (22)$$

Instead of simultaneously finding the optimal external ac- 967  
tions and QoS levels as in the centralized DP operator, we 968  
optimize (22) layer by layer. We rewrite the DP operator in (22) 969  
as in (23), shown at the bottom of the page. 970

For each next state at the lower layers  $(s'_1, \dots, s'_{L-1})$ , the DP 971  
operator at layer  $L$  is 972

$$V_{L-1}(s'_1, \dots, s'_{L-1}) = \max_{\substack{a_L \in A_L, \\ Z_L \in \mathcal{Z}_L}} \left[ R_{\text{in}}(s_L, Z_L) - \lambda_L^a c_L(s_L, a_L) + \gamma \sum_{s'_L \in \mathcal{S}_L} p(s'_L | s_L, Z_L, a_L) V(s'_1, \dots, s'_L) \right]. \quad (24)$$

Then, the optimal external action  $a_L(s'_1, \dots, s'_{L-1})$  and QoS 973  
level  $Z_L(s'_1, \dots, s'_{L-1})$  depend on the next states of the lower 974  
layers. We should note that the optimization in (23) is not 975  
exactly the same as the one in (22), which were analyzed 976  
in Section IV-B. When layer  $L$  performs the optimization 977  
as in (24) for each state  $(s'_1, \dots, s'_{L-1})$ , it sends a message 978  
 $\{V_{L-1}(s'_1, \dots, s'_{L-1}) | \forall (s'_1, \dots, s'_{L-1})\}$  to layer  $L-1$ . At the 979  
same time, the DP operator is reduced as 980

$$\max_{a_1 \in A_1, \dots, a_{L-1} \in A_{L-1}} \left\{ - \sum_{l=1}^{L-1} \lambda_l^a c_l(s_l, a_l) + \sum_{s'_1 \in \mathcal{S}_1, \dots, s'_{L-1} \in \mathcal{S}_{L-1}} \prod_{l=1}^{L-1} p(s'_l | s_l, a_l) V_{L-1}(s'_1, \dots, s'_{L-1}) \right\}. \quad (25)$$

$$\max_{a_1 \in A_1, \dots, a_{L-1} \in A_{L-1}} \left\{ - \sum_{l=1}^{L-1} \lambda_l^a c_l(s_l, a_l) + \sum_{s'_1 \in \mathcal{S}_1, \dots, s'_{L-1} \in \mathcal{S}_{L-1}} \prod_{l=1}^{L-1} p(s'_l | s_l, a_l) \underbrace{\left[ R_{\text{in}}(s_L, Z_L) - \lambda_L^a c_L(s_L, a_L) + \gamma \sum_{s'_L \in \mathcal{S}_L} p(s'_L | s_L, Z_L, a_L) V(s'_1, \dots, s'_L) \right]}_{\text{DP operator at layer } L} \right\} \quad (23)$$

$$\max_{a_1 \in A_1, \dots, a_{L-2} \in A_{L-2}} \left\{ - \sum_{l=1}^{L-2} \lambda_l^a c_l(s_l, a_l) + \sum_{s'_1 \in \mathcal{S}_1, \dots, s'_{L-2} \in \mathcal{S}_{L-2}} \prod_{l=1}^{L-2} p(s'_l | s_l, a_l) \right. \\ \left. \times \underbrace{\max_{a_{L-1} \in A_{L-1}} \left[ -\lambda_{L-1}^a c_{L-1}(s_{L-1}, a_{L-1}) + \sum_{s'_{L-1} \in \mathcal{S}_{L-1}} p(s'_{L-1} | s_{L-1}, a_{L-1}) V_{L-1}(s'_1, \dots, s'_{L-1}) \right]}_{\text{value iteration of layer } L-1} \right\} \quad (26)$$

981 Similar to (23), the optimization in (25) is rewritten in (26),  
982 shown at the top of the page.

983 For each next state at the lower layers  $(s'_1, \dots, s'_{L-2})$ , the DP  
984 operator at layer  $L-1$  is

$$V_{L-2}(s'_1, \dots, s'_{L-2}) \\ = \max_{a_{L-1} \in A_{L-1}} \left[ -\lambda_{L-1}^a c_{L-1}(s_{L-1}, a_{L-1}) \right. \\ \left. + \sum_{s'_{L-1} \in \mathcal{S}_{L-1}} p(s'_{L-1} | s_{L-1}, a_{L-1}) \right. \\ \left. \times V_{L-1}(s'_1, \dots, s'_{L-1}) \right]. \quad (27)$$

985 Then, the message from layer  $L-1$  to layer  $L-2$  is  
986  $\{V_{L-2}(s'_1, \dots, s'_{L-2}) | \forall (s'_1, \dots, s'_{L-2})\}$ .

987 Similarly, for each state  $(s'_1, \dots, s'_l)$ , layer  $l$  performs the DP  
988 operator as follows:

$$V_{l-1}(s'_1, \dots, s'_{l-1}) \\ = \max_{a_l \in A_l} \left[ -\lambda_l^a c_l(s_l, a_l) + \sum_{s'_l \in \mathcal{S}_l} p(s'_l | s_l, a_l) V_l(s'_1, \dots, s'_l) \right]. \quad (28)$$

989 We can interpret  $V_{l-1}(s'_1, \dots, s'_{l-1})$  as a state-value func-  
990 tion of state  $(s'_1, \dots, s'_{l-1})$  seen at layer  $l-1$ . The message  
991 exchanged from layer  $l$  to layer  $l-1$  is  $\{V_{l-1}(s'_1, \dots, s'_{l-1}) |$   
992  $\forall (s'_1, \dots, s'_{l-1})\}$ .

993 At layer 1, the DP operator is

$$V(s) = \max_{a_1 \in A_1} \left[ -\lambda_1^a c_1(s_1, a_1) + \sum_{s'_1 \in \mathcal{S}_1} p(s'_1 | s_1, a_1) V_1(s'_1) \right]. \quad (29)$$

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